

Lecture 2: Knowing Data and Its Types

1. Introduction to Data Objects and Attributes

In data mining, we analyze **data sets** composed of **data objects**. A data object represents an entity such as a customer, product, or patient and is described by **attributes**.

- **Data Object:** Also known as a *sample, instance, record, or tuple*.
- **Attribute:** A data field representing a characteristic of a data object (e.g., *age, height, price*). Also called *variable, feature, or dimension*.

2- Types of Attributes:

Attributes can be classified into the following types:

1. **Nominal**
2. **Binary**
3. **Ordinal**
4. **Numeric**

1- Nominal Attributes

- **Definition:** Attributes whose values are symbols or names representing categories. The values have no meaningful order.
- **Examples:**
 - **hair_color:** black, brown, blond, red
 - **marital_status:** single, married, divorced
 - **occupation:** teacher, engineer, doctor
- **Properties:**
 - Values are categories or states.
 - Mathematical operations are not meaningful.
 - Mode (most frequent value) is a useful measure.

2- Binary Attributes

- **Definition:** Nominal attributes with only two possible states: 0 or 1.
- **Examples:**
 - **smoker:** yes (1) or no (0)
 - **medical_test:** positive (1) or negative (0)
- **Types:**
 - **Symmetric:** Both states are equally important (e.g., *gender*).
 - **Asymmetric:** One state is more important than the other (e.g., *HIV test result*).

3- Ordinal Attributes

- **Definition:** Attributes with values that have a meaningful order or ranking, but the differences between values are not known.
- **Examples:**
 - **drink_size:** small, medium, large
 - **education_level:** high school, bachelor, master, PhD
 - **customer_rating:** poor, fair, good, excellent
- **Properties:**
 - Order is meaningful.
 - Differences between values are not quantifiable.
 - Median and mode are appropriate measures of central tendency.

4- Numeric Attributes

- **Definition:** Quantitative attributes represented by integer or real values.

- **Types:**
 - **Interval-Scaled:**
 - Measured on a scale with equal units.
 - Differences are meaningful, but ratios are not.
 - **Example:** Temperature in Celsius or Fahrenheit.
 - **Ratio-Scaled:**
 - Has a true zero point.
 - Ratios between values are meaningful.
 - **Examples:** Height, weight, age, income.

5- Discrete vs. Continuous Attributes

- **Discrete Attribute:**
 - Has a finite or countably infinite set of values.
 - **Examples:** customer_ID, zip_code, number_of_children.
- **Continuous Attribute:**
 - Has real numbers as values.
 - **Examples:** height, weight, temperature.

6- Basic Statistical Descriptions of Data

To understand data, we use **statistical measures**:

a. Measures of Central Tendency

- **Mean:** The average value.
- **Median:** The middle value in a sorted list.
- **Mode:** The most frequently occurring value.
- **Midrange:** The average of the largest and smallest values.

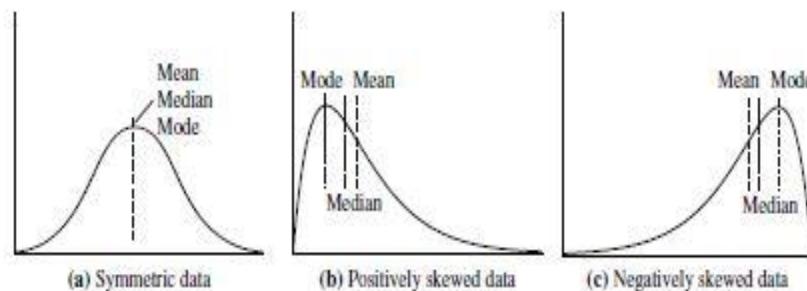


Figure 2.1 Mean, median, and mode of symmetric versus positively and negatively skewed data.

b. Measures of Data Dispersion

- **Range:** Difference between max and min values.
- **Quartiles:** Q1 (25th percentile), Q2 (median), Q3 (75th percentile).
- **Interquartile Range (IQR):** $IQR = Q3 - Q1$.

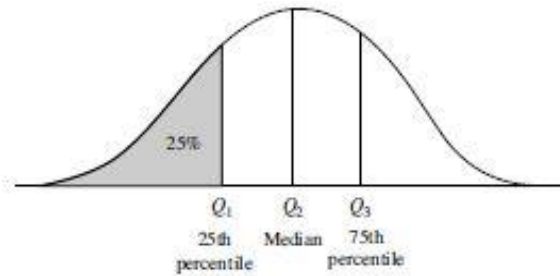


Figure 2.2 A plot of the data distribution for some attribute X . The quantiles plotted are quartiles. The three quartiles divide the distribution into four equal-size consecutive subsets. The second quartile corresponds to the median.

- **Variance & Standard Deviation:** Measures of data spread.
- **Five-Number Summary:** Min, Q_1 , Median, Q_3 , Max.

c. Graphic Displays

- **Boxplots:** Visualize five-number summary and outliers.

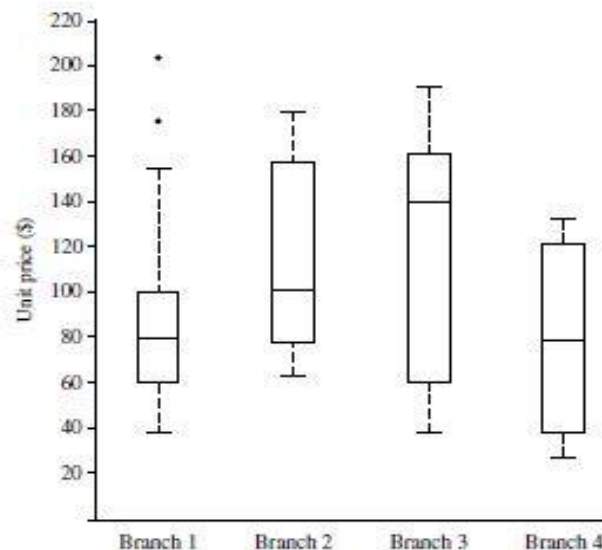


Figure 2.3 Boxplot for the unit price data for items sold at four branches of *AllElectronics* during a given time period.

- **Histograms:** Show frequency distributions.

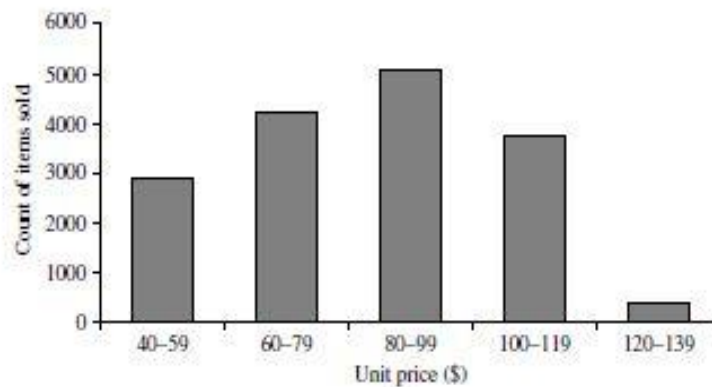


Figure 2.6 A histogram for the Table 2.1 data set.

- **Scatter Plots:** Display relationships between two numeric attributes.

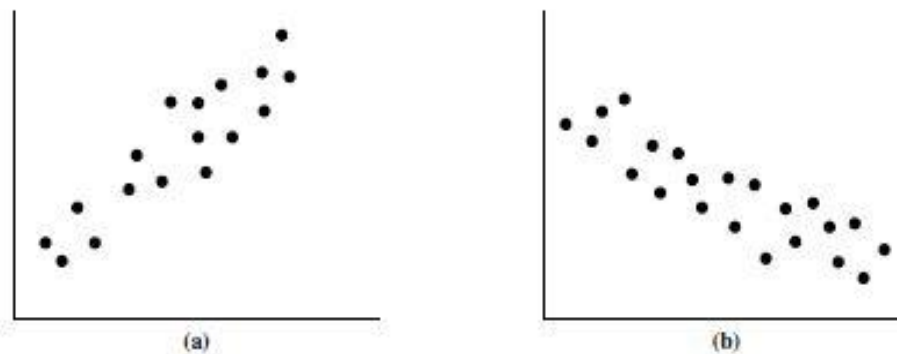


Figure 2.8 Scatter plots can be used to find (a) positive or (b) negative correlations between attributes.

- **Quantile Plots:** Compare distributions.

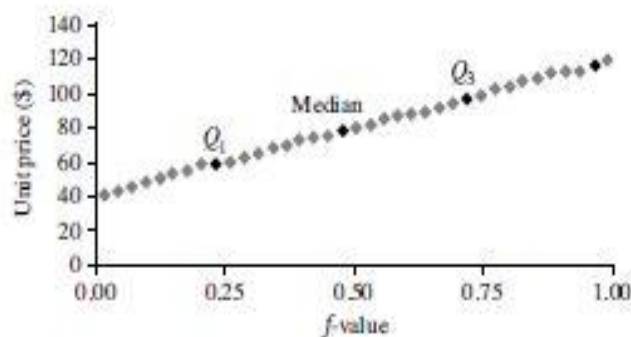


Figure 2.4 A quantile plot for the unit price data of Table 2.1.

8. Data Visualization Techniques

Visualization helps in understanding data patterns and relationships.

a. Pixel-Oriented Techniques

- Each attribute value is represented by a colored pixel.

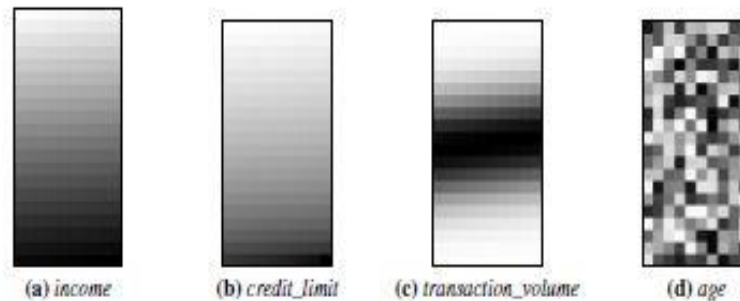


Figure 2.10 Pixel-oriented visualization of four attributes by sorting all customers in *income* ascending order.

b. Geometric Projection Techniques

- Scatter Plots:** 2-D or 3-D plots of data points.

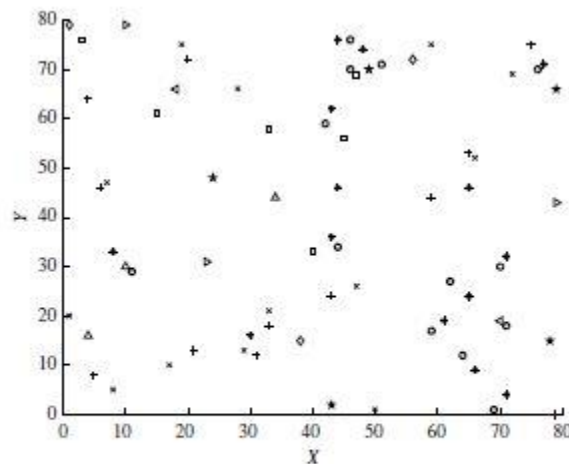


Figure 2.13 Visualization of a 2-D data set using a scatter plot. Source: www.cs.sfu.ca/jpei/publications/rareevent-geoinformatica06.pdf.

- Parallel Coordinates:** Each attribute is represented by a parallel axis.

c. Icon-Based Techniques

- Chernoff Faces:** Represent multi-dimensional data using facial features.

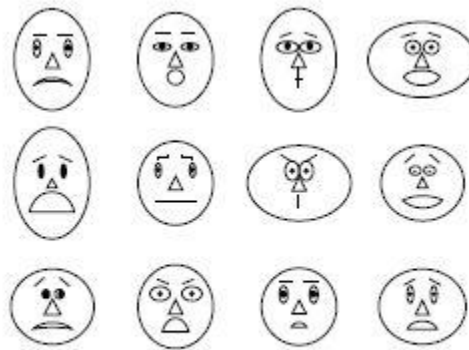


Figure 2.17 Chernoff faces. Each face represents an n -dimensional data point ($n \leq 18$).

- **Stick Figures:** Use limb angles and lengths to represent attributes.



Figure 2.18 Census data represented using stick figures. Source: Professor G. Grinstein, Department of Computer Science, University of Massachusetts at Lowell.

d. Hierarchical Techniques

- **Tree-maps:** Display hierarchical data as nested rectangles.



Figure 2.20 Newsmap: Use of tree-maps to visualize Google news headline stories. Source: www.cs.umd.edu/class/spring2005/cmsc838s/viz4all/ss/newsmap.png.

- **Worlds-within-Worlds (n-Vision):** Explore high-dimensional data in multiple levels.

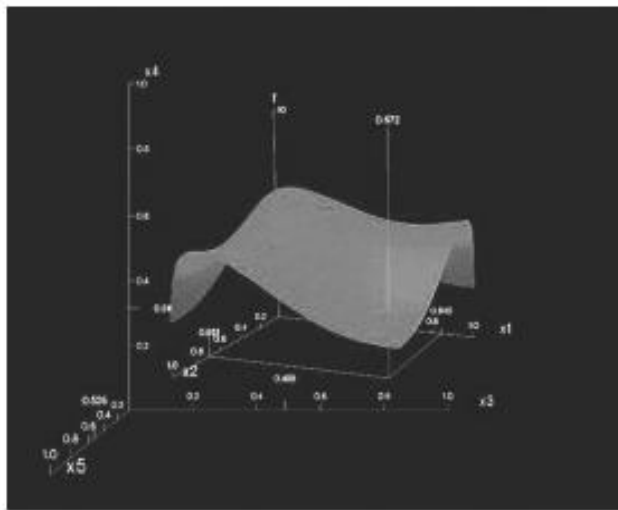


Figure 2.19 "Worlds-within-Worlds" (also known as *n*-Vision). Source: <http://graphics.cs.columbia.edu/projects/AutoVisual/images/1.dipstick.5.gif>.

9. Measuring Data Similarity and Dissimilarity

In many data mining tasks (e.g., clustering, classification), we need to measure how similar or dissimilar objects are.

a. Data Structures

- **Data Matrix:** $n \times p$ matrix storing n objects with p attributes.

Data matrix (or object-by-attribute structure): This structure stores the n data objects in the form of a relational table, or n -by- p matrix (n objects \times p attributes):

$$\begin{bmatrix} x_{11} & \cdots & x_{1f} & \cdots & x_{1p} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ x_{i1} & \cdots & x_{if} & \cdots & x_{ip} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ x_{n1} & \cdots & x_{nf} & \cdots & x_{np} \end{bmatrix}. \quad (2.8)$$

- **Dissimilarity Matrix:** $n \times n$ matrix storing pairwise dissimilarities.
 - **Dissimilarity matrix** (or *object-by-object structure*): This structure stores a collection of proximities that are available for all pairs of n objects. It is often represented by an n -by- n table:

$$\begin{bmatrix} 0 & & & & \\ d(2,1) & 0 & & & \\ d(3,1) & d(3,2) & 0 & & \\ \vdots & \vdots & \vdots & \ddots & \\ d(n,1) & d(n,2) & \dots & \dots & 0 \end{bmatrix}, \quad (2.9)$$

where $d(i, j)$ is the measured **dissimilarity** or "difference" between objects i and j . In general, $d(i, j)$ is a non-negative number that is close to 0 when objects i and j are highly similar or "near" each other, and becomes larger the more they differ. Note that $d(i, i) = 0$; that is, the difference between an object and itself is 0. Furthermore, $d(i, j) = d(j, i)$. (For readability, we do not show the $d(j, i)$ entries; the matrix is symmetric.) Measures of dissimilarity are discussed throughout the remainder of this chapter.

b. Proximity Measures by Attribute Type

- **Nominal Attributes:**
 - $d(i, j) = p - mp$, where m is the number of matches.
- **Binary Attributes:**
 - **Symmetric:** $d(i, j) = r + sq + r + s + t$
 - **Asymmetric (Jaccard Coefficient):** $d(i, j) = r + sq + r + s$
- **Numeric Attributes:**
 - **Euclidean Distance:** $d(i, j) = \sum_{k=1}^p (x_{ik} - x_{jk})^2$
 - **Manhattan Distance:** $d(i, j) = \sum_{k=1}^p |x_{ik} - x_{jk}|$
 - **Minkowski Distance:** $d(i, j) = (\sum_{k=1}^p |x_{ik} - x_{jk}|^h)^{1/h}$
- **Ordinal Attributes:**
 - Replace values with ranks, normalize, then use numeric distance measures.
- **Mixed Types:**
 - Combine dissimilarities from different attribute types into a single measure.
- **Cosine Similarity** (for text or sparse data):
 - $\text{sim}(x, y) = \frac{x \cdot y}{\|x\| \|y\|}$

Summary

- Understanding **data types** is essential for choosing the right data mining techniques.
- **Statistical descriptions** and **visualization** help explore data characteristics.
- **Similarity and dissimilarity measures** are crucial for clustering, classification, and outlier detection.

By knowing your data and its types, you can preprocess it effectively and apply appropriate mining methods to extract meaningful patterns.