

Sets and Operations

A set is a collection of objects without repetition.

$$A = \{1, 2, 4, 5\}$$

$$A = \{x/x \text{ is integer } 2 \leq x \leq 20\}$$

Empty set $\rightarrow \emptyset$

$$A = \{1, 2, 3, \dots, 20\} \rightarrow \text{Finite set}$$

$$N = \{1, 2, 3, \dots\} \rightarrow \text{Infinite set}$$

Binary operations

1. $A \cup B$, **union** of A and B, is $\{x / x \text{ is in A or } x \text{ is in B}\}$
2. $A \cap B$, the **intersection** of A and B, is $\{x / x \text{ is in A and } x \text{ is in B}\}$
3. A / B , the **difference** of A and B, is $\{x / x \text{ is in A and } x \text{ is not in B}\}$
4. $A \times B$, the **Cartesian product** of A and B, is the set of ordered pairs (a, b) such that a is in A and b is in B.
5. 2^A , the **power set** of A, is the set of all subsets of A.

6. Equality

$$A = B, \text{ iff}$$

$$A \subseteq B$$

$$B \subseteq A$$

Example:

Let $A = \{1, 2\}$, $B = \{2, 3\}$ then

$$A \cup B = \{1, 2, 3\}$$

$$A \cap B = \{2\}$$

$$A / B = \{1\} \quad \text{OR Sometimes this is also written as } A - B$$

$$A \times B = \{(1, 2), (1, 3), (2, 2), (2, 3)\}$$

$$\text{And } 2^A = \{\emptyset, \{1\}, \{2\}, \{1, 2\}\}$$

Note:

If A and B have n, m members respectively, then $A \times B$ has nm members and 2^A has 2^n members.

Remark:

We can construct a new language by using any one of the above operations.