## NFA (Non-Deterministic finite automata)

> NFA stands for non-deterministic finite automata. It is easy to construct an NFA than DFA for a given regular language.
> The finite automata are called NFA when there exist many paths for specific input from the current state to the next state.
$>$ Every NFA is not DFA, but each NFA can be translated into DFA.
> NFA is defined in the same way as DFA but with the following two exceptions, it contains multiple next states, and it contains $\varepsilon$ transition.

NFA also has five tuples same as DFA, but with different transition functions, as shown as follows:

1. Q: finite set of states
2. $\sum$ : finite set of the input symbol
3. q 0 : initial state
4. F : final state
5. $\delta$ : Transition function
note: $\delta$ in NFA $\delta: Q \times \sum \rightarrow 2^{\mathrm{Q}}$, but in DFA $\delta: \mathrm{Q} \times \sum \rightarrow \mathrm{Q}$

Ex: NFA with $\sum=\{0,1\}$ and accepts all strings with 01.

$\delta$-table:

| state | 0 | 1 |
| :---: | :---: | :---: |
| $\rightarrow \mathrm{q} 0$ | q 1 | $\varepsilon$ |
| q 1 | $\varepsilon$ | q 2 |
| ${ }^{*} \mathrm{q} 2$ | q 2 | q 2 |

## Ex:

$L=\left\{1 x \mid x \in\{0,1\}^{*}\right\}$ in DFA, NFA machines.

## DFA:




* A nondeterministic finite automata (NFA) allows transitions on a symbol from one state to possibly more than one other state.


Allow $\varepsilon$-transitions from one state to another whereby we can move from the first state to the second without inputting the next character.


* In an NFA a state may have zero, one, or more exiting arrows for each symbol of alphabet.

$$
\sum=\{\mathrm{a}, \mathrm{~b}, \mathrm{c}\}
$$



## Basic NFA ideas

$\checkmark$ Start in the start state.
$\checkmark$ If any $\varepsilon$ transition, clone a machine for each.
$\checkmark$ Read a symbol, and clone a machine for each matching transition.
$\checkmark$ If a symbol is read and there is no way to exit from a state, that machine dies.
$\checkmark$ At the end of input if any machine accepts then accept.


Ex: Build NFA machine that accepts strings containing either 101 or 11 as a substring for $\left.\sum=0,1\right\}$, and read 010110 .


Read: 010110


Equivalence of machines
Definition:
Machine $\mathrm{M}_{1}$ is equivalent to machine $\mathrm{M}_{2}$ if $\mathrm{L}\left(\mathrm{M}_{1}\right)=\mathrm{L}\left(\mathrm{M}_{2}\right)$
Example of equivalent machines:
$L=\left\{1 x \mid x \in\{0,1\}^{*}\right\}$
DFA:
NFA:



Any language $L$ accepted by a DFA is also accepted by an NFA

## Proof by construction:

given an arbitrary NFA $\mathbf{N}$, construct an equivalent DFA D
suppose that N of the $\sum=\{0,1\}$ is as follows:


Solution:



