How to construct DFA for languages consisting of strings starting with a particular substring?

1. Decide the strings for which DFA will be constructed.
2. Determine the minimum number of states required in the DFA No.of states=n+2
n : length of the string.
3. Construct a DFA for the strings decided in 2.
4. Send all the left possible combinations to the dead state. Do not send the left possible combinations over starting state.

Ex: Draw a DFA machine for the language accepting strings starting with ' 1 ' over input alphabets $\Sigma=\{0,1\}$.

Sol:


Ex: Draw a DFA machine for the language accepting strings starting with '101' over input alphabets $\Sigma=\{0,1\}$.

Sol:


Example of constructing DFA for languages consisting of specified substrings anywhere in the word:

Draw a DFA machine for the language accepting substrings 'aab' over input alphabets $\sum=\{a, b, c\}$.

Sol:


Ex: Design DFA which checks whether a given binary number is divisible by 3.

Sol:
.: binary number $\rightarrow \Sigma=\{0,1\}$.

| Decimal no. | Binary no. | Remainder | States Remaider |
| :---: | :---: | :---: | :---: |
| 0 | 0000 | 0 | q 0 |
| 1 | 0001 | 1 | q 1 |
| 2 | 0010 | 2 | q 2 |
| 3 | 0011 | 0 | q 0 |
| 4 | 0100 | 1 | q 1 |
| 5 | 0101 | 2 | q 2 |
| 6 | 0110 | 0 | q 0 |
| 7 | 0111 | 1 | q 1 |
| 8 | 1000 | 2 | q 2 |
| 9 | 1001 | 0 | q 0 |



Ex1: Construct a DFA, that accepts set of all strings over $\Sigma=\{a, b\}$ of length 2.
i.e $|w|=2 \rightarrow L=\{a a, a b, b a, b b\}$

Ex2: Construct a DFA, that accepts set of all strings over $\Sigma=\{a, b\}$ of length at least 2.
i.e $|w|>=2$

Ex3: Draw a DFA for the language accepting string starting with 'ab' over input alphabets $\sum=\{\mathrm{a}, \mathrm{b}\}$.

Ex4: Draw a DFA for the language accepting string ending with 'abba' over input alphabets $\sum=\{\mathrm{a}, \mathrm{b}\}$.

Ex5: Design DFA which checks whether a given binary number is divisible by 4.

