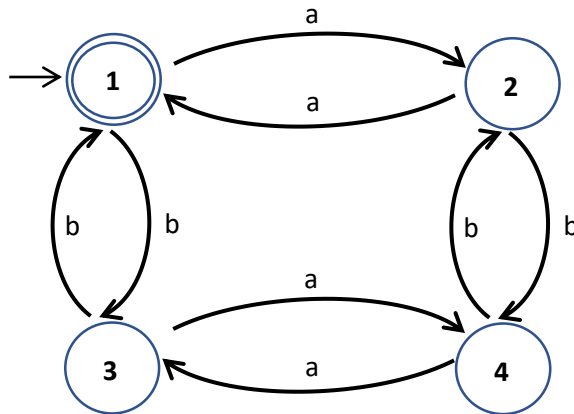


Ex: Build an FA that accepts only the language of all words that must have (even-even) from the alphabet a, b?

$L = \{w \mid w \text{ has even no. of a's and even no. of b's}\}$

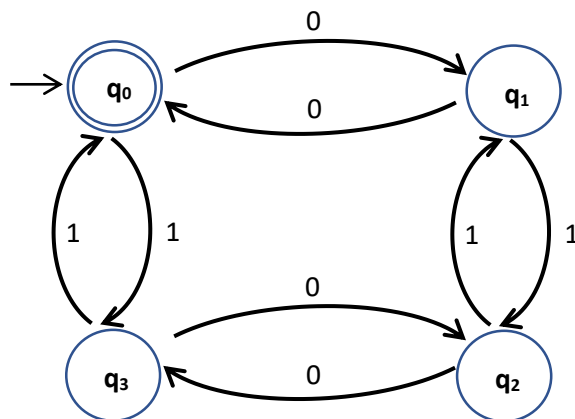
$\Sigma = \{a, b\}$



Find the following:

- (even a-odd b)
- (odd a-even b)
- (odd a-odd b)

Ex: let a transition follow:



Find FSA acceptor and check if the string (110101) is an input string to M acceptor or not?

Sol:

$$M = \langle Q, \Sigma, S, F, \delta \rangle$$

$$Q = \{q_0, q_1, q_2, q_3\}$$

$$\Sigma = \{0, 1\}$$

$$S = q_0$$

$$F = \{q_0\}$$

$$\delta(q_0, 0) = q_1$$

$$\delta(q_0, 1) = q_3$$

$$\delta(q_1, 0) = q_0$$

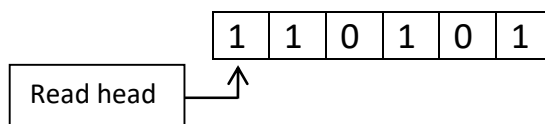
$$\delta(q_1, 1) = q_2$$

$$\delta(q_2, 0) = q_3$$

$$\delta(q_2, 1) = q_1$$

$$\delta(q_3, 0) = q_2$$

$$\delta(q_3, 1) = q_0$$



$$\delta(q_0, 1) = q_3$$

$$\delta(q_3, 1) = q_0$$

$$\delta(q_0, 0) = q_1$$

$$\delta(q_1, 1) = q_2$$

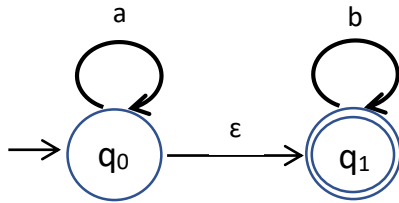
$$\delta(q_2, 0) = q_3$$

$$\delta(q_3, 1) = q_0 \text{ the final state}$$

$\therefore$  this string is the acceptor.

Ex: Construct a machine for the following language:  $L = \{ a^*b^* \}$

Sol:



$M = \langle Q, \Sigma, S, F, \delta \rangle$

$Q = \{ q_0, q_1 \}$

$\Sigma = \{ a, b, \epsilon \}$

$S = q_0$

$F = \{ q_1 \}$

$\delta(q_0, a) = q_0$

$\delta(q_0, \epsilon) = q_1$

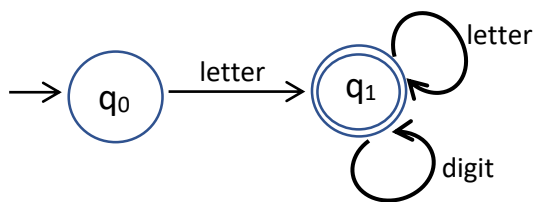
$\delta(q_1, b) = q_1$

$\delta$ - table

|       |             |             |             |
|-------|-------------|-------------|-------------|
|       | a           | b           | $\epsilon$  |
| $q_0$ | $q_0$       | $\emptyset$ | $q_1$       |
| $q_1$ | $\emptyset$ | $q_1$       | $\emptyset$ |

Ex: Build DFSA for identifier?

Sol:



$M = \langle Q, \Sigma, S, F, \delta \rangle$

$Q = \{ q_0, q_1 \}$

$\Sigma = \{ \text{letter}, \text{digit} \}$

$S = q_0$

$F = \{ q_1 \}$

$$\delta(q_0, \text{letter}) = q_1$$

$$\delta(q_1, \text{letter}) = q_1$$

$$\delta(q_1, \text{digit}) = q_1$$

 $\delta$ - table

|       | letter | digit       |
|-------|--------|-------------|
| $q_0$ | $q_1$  | $\emptyset$ |
| $q_1$ | $q_1$  | $q_1$       |

- Prove that string (as1) is accepted by the FSA?

$$\delta(q_0, a) = q_1$$

$$\delta(q_1, s) = q_1$$

$$\delta(q_1, 1) = q_1$$

∴ the string is accept.

- Which of the strings is accepted by the above identifier machine?
1. ab
  2. ab2
  3. 1ab
  4. a1b