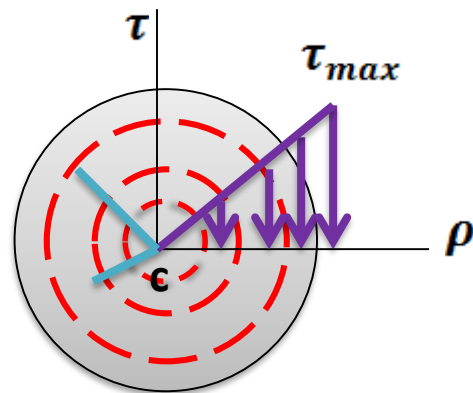
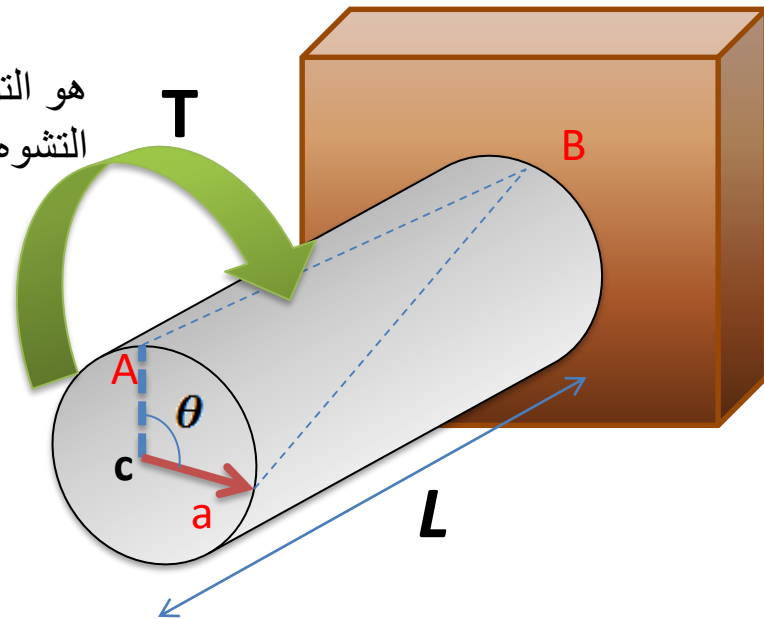
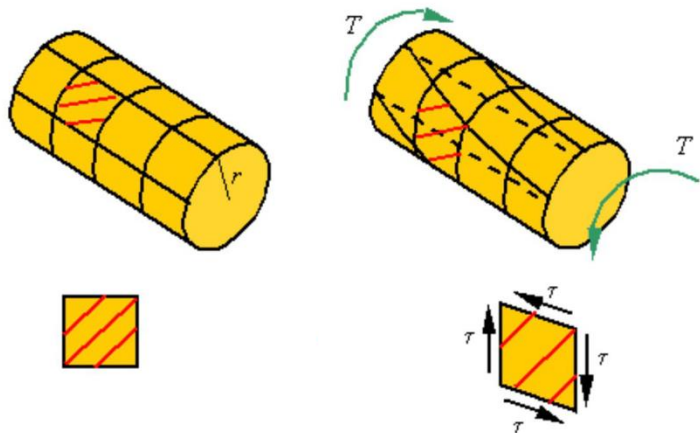


Torsion

Torsion :

هو التواء جسم ناتج عن عزم حول المحور الطولي للجسم. وإنه نوع من التشوه.



Shearing stress :

$$\tau = \frac{T \rho}{J}$$

$$\tau_{max} = \frac{T r}{J}$$

$$\tau_{max} = \frac{T r}{J}$$

τ_{max} = shearing stress(pa)

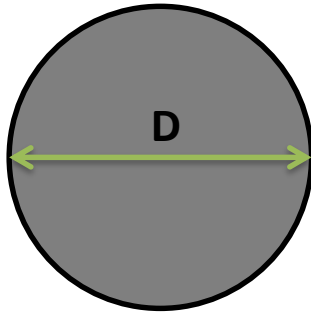
T = Torque (twisting moment)(N.m)

r = raduis of shaft (m)

J = polar moment of interia of scetion (m⁴)

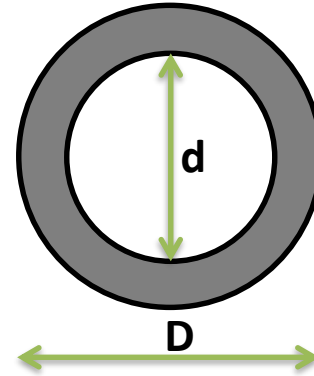
J

Solid shaft



$$J = \frac{\pi}{32} D^4$$

hollow shaft



$$J = \frac{\pi}{32} (D^4 - d^4)$$

Angle of twist :

$$\theta = \frac{TL}{JG}$$

rad. ($3\pi, 5\pi, 20\pi$)
deg. ($^{\circ}$) ($45^{\circ}, 60^{\circ}, 75^{\circ}$)

θ = angle of twist (rad)

T = Torque (twisting moment) (N.m)

L = length of shaft (m)

J = polar moment of inertia of section (m^4)

G = modulus of rigidity for material (Gpa)

Shear strain :

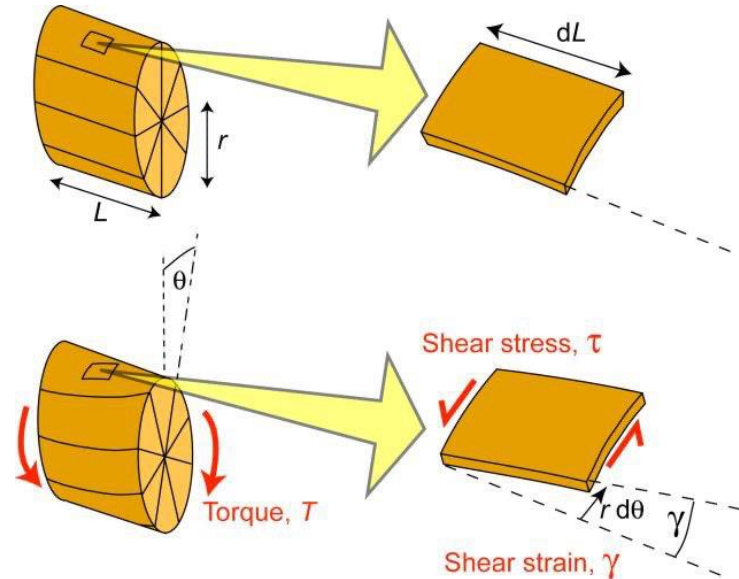
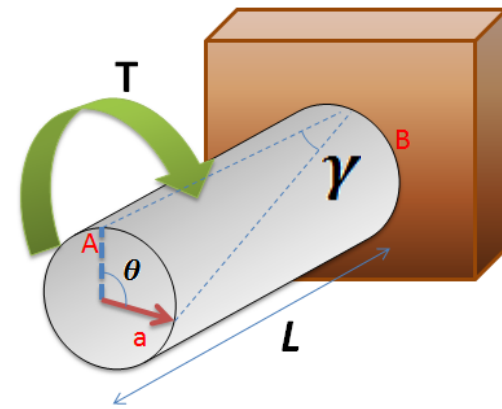
$$\gamma = \frac{r\theta}{L}$$

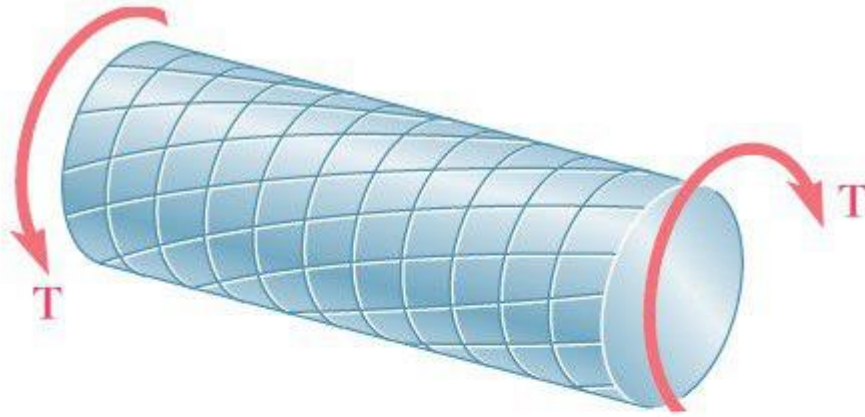
γ = Shear strain

θ = angle of twist (rad)

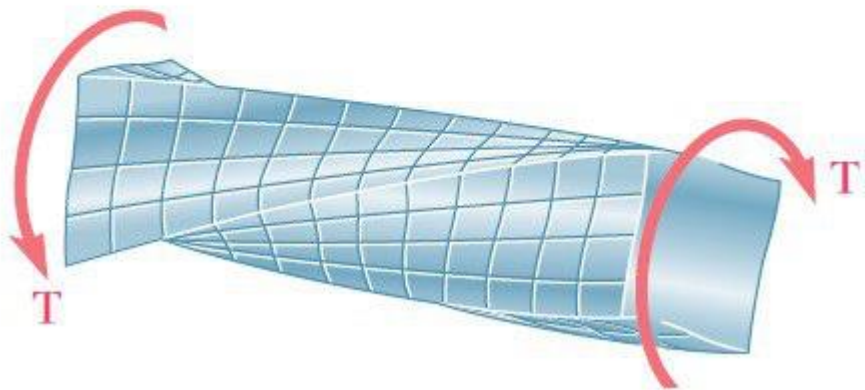
r = radius of shaft (m)

L = length of shaft (m)





Axisymmetric



Not Axisymmetric



Power transmitted by the shaft : الطاقة المنقولة بواسطة العمود

A shaft rotating with a constant angular velocity (in radius per second)
is being acted by a twisting moment (T).

عمود يدور بسرعة زاوية ثابتة (نصف قطر في الثانية) يتأثر عزم التواء (T).

$$P = W T$$

$$W = 2\pi f$$

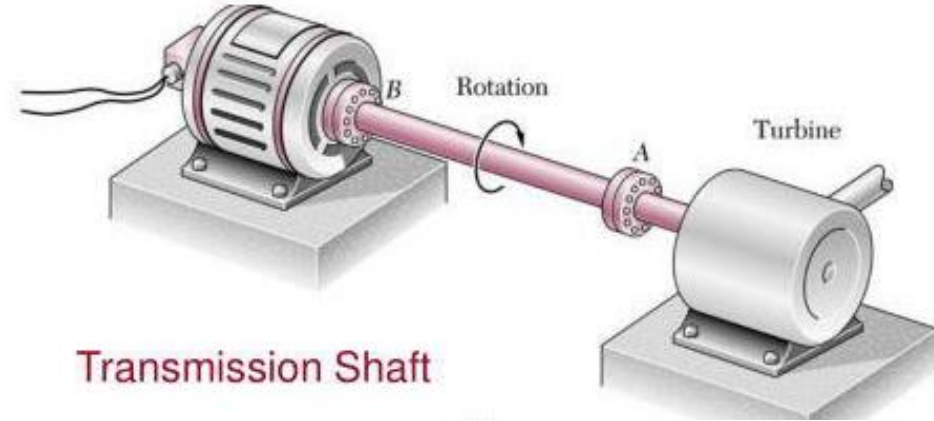
$W =$ angular speed of rotation of the shaft

$$P = 2\pi f T$$

$P =$ the power in watt (W)

$f =$ is number of revloution per second (HZ)

$T =$ Torque (twisting moment)(N.m)



$$HZ = \frac{1}{sec} \text{ (cycle per second)}$$



Shearing stress :

$$\tau_{max} = \frac{T r}{J}$$

$$J = \frac{\pi}{32} D^4$$

$$J = \frac{\pi}{32} (D^4 - d^4)$$

Angle of twist :

$$\theta = \frac{T L}{J G}$$

Power transmitted by the shaft :

$$P = 2\pi f T$$

Shear strain :

$$\gamma = \frac{r\theta}{L}$$



مثال // بالنسبة للعمود الأسطواني الموضح ، حدد الحد الأقصى. لإجهاد القص
 الناجم عن عزم الدوران ، اذ علمت ان معامل الصلابة هو $G = 80 \text{Gpa}$ ، أوجد
 أيضاً زاوية الالتواء (deg.) وإجهاد القص في العمود الصلب؟

Sol:

$$\tau_{max} = \frac{T r}{J} = \frac{T (\frac{D}{2})}{\frac{\pi}{32} D^4}$$

$$\tau_{max} = \frac{16T}{\pi D^3}$$

$$\tau_{max} = \frac{16(800 \times 10^3)}{\pi(36)^3} \left(\frac{\text{N. mm}}{\text{mm}^3} \right) = 87.3 \text{ N/mm}^2$$

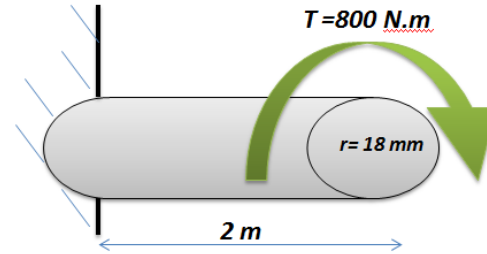
$$\tau_{max} = 87.3 \text{ Mpa}$$

$$\theta = \frac{T L}{G J}$$

$$\theta = \frac{(800 \times 10^3)(2 \times 10^3)}{(80 \times 10^3) \left(\frac{\pi}{32} \right) (36)^4} \left(\frac{\text{N. mm. mm}}{\text{mm}^2 \cdot \text{mm}^4} \right)$$

$$\theta = 0.12 \text{ rad}$$

$$\theta = 0.12 \left(\frac{180}{\pi} \right) = 6.87^\circ$$



80Gpa
 $80 \times 10^3 \text{Mpa}$
 $80 \times 10^3 \text{N/mm}^2$

$$\gamma = \frac{r\theta}{L}$$

$$\gamma = \frac{18(0.12)}{2 \times 10^3} = 108 \times 10^{-5}$$



