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## Bifurcation and Chaos in indirect field-oriented controlled induction motor drive system

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**Abstract** In this paper, the higher-order three-phase indirect field-oriented controlled (IFOC) 8 induction motor is modeled in synchronous reference frame. The IFOC induction motor is 9 analyzed numerically to investigate the system behavior due to control parameters change. 10 The slip speed compensator, integral, and proportional gains variations of the speed loop 11 controller are used to confirm the system dynamics. The simulation results show that the 12 chaos behavior is noted in small region of the slip speed compensator gain which is difficult 13 to be observed through the dominant limit cycles and fixed-point solutions. The effects of the 14 integral and proportional gains change on the system dynamic are verified. Also, the system 15 exhibits period-doubling bifurcation (period-2, period-4, period-8, and period-16) route to 16 chaos. The bifurcation diagram and Lyapunov exponent spectrum assign these situations. The 17 phase portrait and time response results are also presented. The system has multistability and 18 coexistence of different attractors for the same system parameters as represented in the basins 19 of attractions plots. 20

## 21 1 Introduction

Indirect field-oriented controlled (IFOC) [1-6] induction motor (IM) is generally utilized 22 in industrial applications for its high torque performance. The parameters of motor may 23 be changed due to aging and environmental conditions, temperature changes and levels of 24 saturation of IM which maybe lead to the variation of the dynamic and the steady state of the 25 drive system [7]. Also, estimation errors diverge these parameters from its real value [8]. In 26 Ref. [9] and Ref. [10], the PI speed controller was tuned in order to prevent the occurrence 27 of saddle-node bifurcation (SNB) and Hopf bifurcation (HB) in IFOC induction motor. In 28 Ref.[11], the PI speed controller was also tuned theoretically to avoid HB, and the results 29 were validated with some simulation proof. The occurrence of co-dimension-two bifurcation 30 phenomena, such as a Bogdanov-Takens bifurcation (BTB) as well as HB, was provided in 31 [12]. Zero Hopf bifurcation (ZHB) was found in [13] which depends on the PI speed controller 32 gain. HB occurrence was proved [14]; they used time-delayed state feedback criterion to 33

avoid HB which was validated numerically. The speed chaotification was confirmed by both

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simulation and experimental results for periodic speed command by tuning the gain of the compensator for the resistance change due to prolonged operation [15]. By using numerical analysis in [16], a SNB was observed at underestimation of rotor resistance; besides, effect of load change on HB was studied where BTB and ZHB phenomenon were also noted with variations of PI speed loop gain. Simulation and experiment results (for SNB and HB) were also offered.

In the studies [9–14], with ignoring stator current dynamics and less comprehensive load-41 ing status, lower-order IM model was relied on. The results in the studies [9–14,16] showed 42 that the general behavior of the system with fixed speed command is the occurrence of the 43 limit cycles (SNB, HB, BTB, and ZHB) in addition to the fixed point. Reference [15] used 44 periodic speed command with and without dc speed offset only to prove the chaotic case, but 45 they did not use fixed speed command, while the fixed speed command is used widely in the 46 industrial applications. The chaotic phenomenon for fixed speed command in dynamics of 47 system was not shown in Refs. [9-14]. 48

In this paper, a bifurcation study on PI-controlled IFOC induction motor is achieved by 49 using a full-order IM model that closes the shortages introduced earlier. Bifurcation situations 50 of IFOCIM are calculated based on linearized model of IFOCIM near the equilibrium point. 51 A numerical analysis is used to investigate period-doubling bifurcation and chaos phenomena 52 with loading condition. The rest of paper is divided into three sections: Sect. 2 deals with 53 IFOCIM system modeling. The scheme of IFOCIM system is introduced, and a mathematical 54 model is derived to investigate the system dynamics. The obtained IFOCIM model consists 55 of eight nonlinear first-order differential equations. Section 3 includes the dynamical analysis 56 of the system. The bifurcation diagrams of the speed of the motor supported with Lyapunov 57 exponent spectrums for a certain ranges of the slip speed compensator gain ( $\alpha$ ) and PI 58 speed integral gain are plotted by using computer simulation to reveal the period-doubling 59 route to chaos. 2D bifurcation diagram of the speed of the motor due to change of PI speed 60 proportional and integral gains is obtained. The period-doubling route to chaos is indicated 61 in the bifurcation diagrams. Finally, conclusion is provided in Sect. 4. 62

## 63 2 Model of IFOCIM drive system

The general closed-loop control diagram of IFOCIM drive is shown in Fig. 1. The speed and flux signals are fed internally, and the direct (d) and quadrature (q) axes current references ( $i_{ds}$ and  $i_{qs}$ ) are produced from the flux and speed PI controllers. The inverter output is applied to IM, while the controller feedback signals are the currents and voltages of the induction motor stator. The synchronous d - q reference frame model of a squirrel-cage induction motor can

<sup>69</sup> be stated according to [3], to have the following full order IM dynamic system:

$$\frac{\mathrm{d}i_{ds}}{\mathrm{d}t} = -\gamma i_{ds} + \omega_e i_{qs} + \zeta \beta \psi_{dr} + \beta \omega_r \psi_{qr} + \frac{v_{ds}}{\sigma L_s} \tag{1}$$

$$\frac{\mathrm{d}i_{qs}}{\mathrm{d}t} = -\omega_e i_{ds} - \gamma i_{qs} - \beta \omega_r \psi_{dr} + \zeta \beta \psi_{qr} + \frac{v_{qs}}{\sigma L_s} \tag{2}$$

$$\frac{\mathrm{d}\psi_{dr}}{\mathrm{d}t} = \zeta L_m i_{ds} - \zeta \psi_{dr} + (\omega_e - \omega_r) \psi_{qr} \tag{3}$$

$$\frac{\mathrm{d}\psi_{qr}}{\mathrm{d}t} = \zeta L_m i_{qs} - (\omega_e - \omega_r) \psi_{dr} - \zeta \psi_{qr} \tag{4}$$

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## Table 1 System parameters definitions

Parameter	Definition	Parameter	Definition
$R_s$	Stator resistance	Р	Number of poles
$L_s$	Stator inductance	J	Rotor inertia
R <sub>r</sub>	Rotor resistance	$B_m$	Viscous friction coefficient
L <sub>r</sub>	Rotor inductance	$T_r$	Rotor time constant
$L_m$	Mutual inductance	$T_l$	Load torque
$\omega_r$	Rotor speed	$\omega_{ m ref}$	Speed reference

81

$$\frac{\mathrm{d}\omega_r}{\mathrm{d}t} = \frac{P}{2J} \left[ \frac{3}{2} \frac{P}{2} \frac{L_m}{L_s} \left( \psi_{dr} i_{qs} - \psi_{qr} i_{ds} \right) - T_L - \frac{2}{P} B_m \omega_r \right] \tag{5}$$

where  $v_{ds}$ ,  $v_{qs}$ ,  $\psi_{dr}$ , and  $\psi_{qr}$  are the stator voltage and the rotor fluxes in synchronous direct and quadrature axis reference frame referred to stator, respectively;  $\omega_e$  is the angular synchronous speed of the motor,  $\sigma = 1 - \frac{L_m^2}{L_s L_r}$ ,  $T_r = \frac{L_r}{R_r}$ ,  $\gamma = \frac{R_s}{\sigma L_s} + \frac{1-\sigma}{\sigma T_r}$ ,  $\beta = \frac{L_m}{\sigma L_s L_r}$ , and  $\zeta = \frac{1}{T_r}$ . The motor parameters are listed in Table 1.

To compensate the change in rotor resistance due to prolonged operation, the slip speed  $(\omega_{sl})$  in IFOCIM method is used to be [17]:

$$\omega_{sl} = (\omega_e - \omega_r) = \frac{\alpha}{T_r} L_m T_{re}$$

$$T_{re} = \left( K_{pw} + K_{iw} \int dt \right) (\omega_{ref} - \omega_r)$$
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(8)

$$i_{dref} = \frac{\psi_{dref} + T_r \dot{\psi}_{dref}}{L_m} - \psi_{qr} T_{re}$$

$$i_{qref} = \psi_{dr} T_{re}$$

$$(7)$$

where  $\alpha$  is the gain of the compensator,  $\psi_{dref}$  is the rotor reference flux, and  $K_{p\omega}$  and  $K_{i\omega}$ 84 are the proportional and integral gains of the speed controller, respectively. From Fig. 1, Eqs 85 (1)–(7), and by defining the state variables  $x_1 = i_{ds}$ ,  $x_2 = i_{qs}$ ,  $x_3 = \psi_{dr}$ ,  $x_4 = \psi_{qr}$ ,  $x_5 = \omega_r$ , 86  $x_6 = (K_{pw} + K_{iw} \int dt) (\omega_{ref} - \omega_r), x_7 = \int (i_{dref} - i_{ds}) dt, \text{ and } x_8 = \int (i_{qref} - i_{qs}) dt$ , the 87

higher-order model (HOM) of IFOCIM system can de expressed by the following equations: 88

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$$\dot{x}_{1} = -\gamma x_{1} + \left\lfloor x_{5} + \frac{1}{T_{r}} L_{m} x_{6} \right\rfloor x_{2} + \frac{1}{T_{r}} x_{3}$$

$$+ \beta \frac{L_{r}}{L_{m}} K p d \left[ \frac{1}{L_{m}} \psi_{dref} + \frac{T_{r}}{L_{m}} \dot{\psi}_{dref} - x_{4} x_{6} - x_{1} \right]$$

$$+ \beta x_{5} x_{4} + \beta \frac{L_{r}}{L_{m}} K_{id} x_{7}$$

$$\dot{x}_2 = -\left[x_5 + \frac{\alpha}{T_r}L_m x_6\right]x_1 - \gamma x_2 - \beta x_5 x_3 + \frac{\beta}{T_r}x_4$$

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$$+\beta \frac{L_r}{L_m} K pq [x_3 x_6 - x_2] + \beta \frac{L_r}{L_m} K_{iq} x_8$$
(9)

94 
$$\dot{x}_3 = \frac{L_m}{T_r} x_1 - \frac{1}{T_r} x_3 + \frac{\alpha}{T_r} L_m x_4 x_6$$
 (10)

95 
$$\dot{x}_4 = \frac{L_m}{T_r} x_2 - \frac{1}{T_r} x_4 - \frac{\alpha}{T_r} L_m x_3 x_6$$
 (11)

96 
$$\dot{x}_5 = \frac{P}{2J} \left[ K \left( x_2 x_3 - x_1 x_4 \right) - T_L \right] - \frac{B_m}{J} x_5$$
 (12)

97 
$$\dot{x}_{6} = -K_{pw} \left[ \frac{P}{2J} \left[ K \left( x_{2}x_{3} - x_{1}x_{4} \right) - T_{L} \right] - \frac{B_{m}}{J} x_{5} \right] + K_{iw} \left( \omega_{\text{ref}} - x_{5} \right)$$
(13)

98 
$$\dot{x}_7 = -x_1 - x_4 x_6 + \frac{1}{Lm} \psi_{dref} + \frac{T_r}{L_m} \dot{\psi}_{dref}$$
 (14)

$$\dot{x}_8 = -x_2 + x_3 x_6 \tag{15}$$

where  $K = \frac{3}{2} \frac{P}{2} \frac{L_m}{L_r}$ ,  $K_{pd}$ ,  $K_{id}$ ,  $K_{pq}$ , and  $K_{iq}$  are the proportional and integral gains for the 100  $i_{ds}$ ,  $i_{qs}$  controllers, respectively. 101

#### **3** Dynamical analysis 102

The IM parameters are listed in Table 2 [15], and the PI controller gains are chosen to be 103  $K_{pd} = K_{pq} = 50, K_{id} = K_{iq} = 100, K_{p\omega} = 20, K_{i\omega} = 5, \psi_{dref} = 0.55$  Wb, and  $\alpha$  is 104 selected to be 1.3. The load torque and the speed reference are set to be 3 Nm and 50 rad/sec, 105 106 respectively.

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99 
$$\dot{x}_8 =$$

Parameter	Value	Parameter	Value
Р	4	$L_r$ (H)	0.2235
$R_{s}\left( \Omega ight)$	0.76	$L_m$ (H)	0.2176
$L_{s}(H)$	0.2248	$J (\mathrm{kg}\mathrm{m}^2)$	0.0111
$R_r(\Omega)$	0.675	$B_m$ (Nm/rad/s)	$7.355 \times 10^{-4}$







## 107 3.1 Equilibrium points

Let the notations  $x_i^e$ , i = 1, 2, ..., 8 indicate the equilibrium point states. By considering  $x_5^e = \omega_{\text{ref}}$  and solving Eq. (8) to (15), the values of the states at the equilibrium point can be

110 described as:

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**Author Proof** 

$$X^{e} = \begin{bmatrix} x_{1}^{e} \\ x_{2}^{e} \\ x_{3}^{e} \\ x_{5}^{e} \\ x_{6}^{e} \\ x_{7}^{e} \\ x_{8}^{e} \end{bmatrix} = \begin{bmatrix} \frac{-m \pm \sqrt{m^{2} - 4ln}}{2l} \\ \frac{B_{m}\omega_{ref} + \frac{P}{2}T_{L}}{\alpha \frac{P}{2}K\psi_{dref}} \\ L_{m}x_{1}^{e}(1-\alpha) + \alpha\psi_{dref} \\ L_{m}x_{2}^{e}(1-\alpha) \\ \omega_{ref} \\ \frac{x_{2}^{e}}{x_{3}^{e}} \\ \frac{L_{m}}{\beta L_{r}K_{id}} \left(a_{1}x_{1}^{e} + a_{2}\frac{(x_{2}^{e})^{2}}{x_{3}^{e}} - a_{3}\right) \\ \frac{L_{m}}{\beta L_{r}K_{iq}} \left(\left(b_{1} + b_{2}\frac{x_{2}^{e}}{x_{3}^{e}}\right)x_{1}^{e} + b_{3}\right) \end{bmatrix}$$
(16)

112 where 
$$l = (1 - \alpha)L_m^2$$
,  $m = (2\alpha - 1)L_m\psi_{dref}$ ,  $n = \frac{l(B_m\omega_{ref} + \frac{p}{2}T_L)^2}{(\alpha \frac{p}{2}K\psi_{dref})^2} - \alpha \psi_{dref}^2$ ,  $a_1 = \frac{1}{2}$ 

113 
$$\gamma - \beta \frac{L_m}{T_r} (1 - \alpha) + \frac{\beta L_r}{L_m} K_{pd}, a_2 = \beta L_r (1 - \alpha) K_{pd} - \alpha \frac{L_m}{T_r}, a_3 = (\beta L_m (1 - \alpha) + 1)$$

$$u_{ref} = \frac{\omega_{ref}}{\alpha \frac{L}{2} K \psi_{tref}} + \left(\frac{\omega_{r}}{T_r} + \frac{1}{L_m^2}\right) \psi_{dref}, \ b_1 = \omega_{ref} + \beta \omega_{ref} L_m (1 - \alpha), \ b_2 = \frac{\omega_m}{T_r}, \text{ and}$$

<sup>115</sup> 
$$b_3 = \left(\gamma - \frac{\beta L_m}{T_r} (1 - \alpha)\right) \frac{B_m \omega_{\text{ref}} + \frac{\gamma}{2} I_L}{\alpha \frac{p}{2} K \psi_{\text{dref}}} + \alpha \beta \omega_{\text{ref}} \psi_{\text{dref}}.$$

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From Eq. (16),  $X^e$  is not unique for  $\alpha \neq 1$ , otherwise  $X^e$  has unique solution. The real solution of  $X^e$  is obtained when:

$$\frac{2L_m \left(B_m \omega_{\text{ref}} + \frac{P}{2} T_L\right)}{2L_m \left(B_m \omega_{\text{ref}} + \frac{P}{2} T_L\right) + \frac{P}{2} K \psi_{\text{dref}}^2} \le \alpha \le \frac{2L_m \left(B_m \omega_{\text{ref}} + \frac{P}{2} T_L\right)}{2L_m \left(B_m \omega_{\text{ref}} + \frac{P}{2} T_L\right) - \frac{P}{2} K \psi_{\text{dref}}^2}$$
(17)

According to Eq. (17) and Fig. 2, the real solution is obtained in the range of  $0.61 \le \alpha \le 3.04$ . In the outside of this range of  $\alpha$ , the system does not have real equilibrium points.

## 121 3.2 Stability of equilibrium points

The IM parameters as in Table 2 [15] and PI controller gains are chosen to be  $K_{pd} = K_{pq} =$ 50,  $K_{id} = K_{iq} = 100$ ,  $K_{p\omega} = 20$ ,  $0 \le K_{i\omega} \le 120$ ,  $\psi_{dref} = 0.55$  Wb, and  $\alpha = 1.3$ . According to Eq. (16), the system has two different equilibrium points:

<sup>125</sup>  $X^{e1} = (2.783, 1.446, 0.533, -0.094, 50, 2.71, 0.12, -0.531)^T$ 

 $X^{e2} = (10.697, 1.446, 0.017, -0.094, 50, 86.561, 0.344, -0.13)^T$ 

Based on the linearization theorem, the differential system is described in matrix form close to the equilibrium point as the following:

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$$\dot{X} = J(x) X \tag{18}$$

where J(x) is the Jacobian matrix of the system,  $X = (x_1, x_2, x_3, x_4, x_5, x_6, x_7, x_8)^T$  is the vector of the system variables, and  $\dot{X} = (\dot{x}_1, \dot{x}_2, \dot{x}_3, \dot{x}_4, \dot{x}_5, \dot{x}_6, \dot{x}_7, \dot{x}_8)^T$ 

<sup>132</sup> The Jacobian matrix of the linearized model can be given as:

$$I(x) = \begin{bmatrix} J_{6\times6} & J_{6\times2} \\ J_{2\times6} & 0_{2\times2} \end{bmatrix}$$
(19)

134 where

$$I_{35} \qquad J_{6\times 6} = \begin{bmatrix} -\gamma - c_1 K_{pd} & x_5 + c_2 x_6 & \frac{\beta}{T_r} & \beta x_5 - c_1 K_{pd} x_6 & -x_2 - \beta x_4 & c_2 x_2 - c_1 K_{pd} x_4 \\ -x_5 - c_2 x_6 & -\gamma - c_1 K_{pq} & c_1 K_{pq} x_6 - \beta x_5 & \frac{\beta}{T_r} & x_1 + \beta x_3 & -c_2 x_1 + c_1 K_{pq} x_3 \\ \frac{c_2}{\alpha} & 0 & \frac{-1}{T_r} & c_2 x_6 & 0 & c_2 x_4 \\ 0 & \frac{c_2}{\alpha} & -c_2 x_6 & \frac{-1}{T_r} & 0 & -c_2 x_3 \\ c_4 x_4 & -c_4 x_3 & -c_4 x_2 & c_4 x_1 & -c_3 & 0 \\ c_4 K_{pw} x_4 & -c_4 K_{pw} x_3 & -c_4 K_{pw} x_2 & c_4 K_{pw} x_1 & K_{iw} - c_3 K_{pw} & 0 \end{bmatrix},$$

<sup>136</sup> 
$$J_{6\times 2} = \begin{bmatrix} c_1 K_{id} & 0 & 0 & 0 & 0 \\ 0 & c_1 K_{iq} & 0 & 0 & 0 \end{bmatrix}^T, J_{2\times 6} = \begin{bmatrix} -1 & 0 & 0 & -x_6 & 0 & -x_4 \\ 0 & -1 & x_6 & 0 & 0 & x_3 \end{bmatrix}$$
  
<sup>137</sup>  $c_1 = \beta \frac{L_r}{L_m}, c_2 = \alpha \frac{L_m}{T_r}, c_3 = \frac{B_m}{J}, \text{ and } c_4 = \frac{1.5L_m P^2}{4JL_r}$ 

The eigenvalues of the Jacobian matrix described in Eq.(19) are checked numerically. The equilibrium point  $X^{e1}$  is stable, while  $X^{e2}$  is unstable for  $K_{i\omega} > 106.4$ . For  $K_{i\omega} = 106.4$ , the eigenvalues are listed in Table 3.

141 3.3 Bifurcation diagram

The system specified by Eqs. (8)–(15) has been simulated numerically for different values of the controller parameters. The bifurcation diagram and corresponding Lyapunov exponents (LEs) spectrum as a function of parameter  $\alpha$  are shown in Fig. 3. The parameters are  $K_{pd} =$  $K_{pq} = 50$ ,  $K_{id} = K_{iq} = 100$ ,  $K_{p\omega} = 20$ , and  $\psi_{dref} = 0.55$  Wb. From Fig. 3, one can note that, for a certain value of controller gains with varying of  $\alpha$ , the system bifurcates into period-1, period-2, period-4 and chaotic attractor. For  $K_{i\omega} = 5$  and  $\alpha$  is varied from

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**Fig. 3** Speed bifurcation diagram and Lyapunov exponents due to  $\alpha$  change at  $K_{pd} = K_{pq} = 50$ ,  $K_{id} = K_{iq} = 100$ , and  $K_{p\omega} = 20$  **a** bifurcation diagram for  $K_{i\omega} = 5$ , **b** corresponding Lyapunov exponents, **c** bifurcation diagram for  $K_{i\omega} = 90$  and **d** corresponding Lyapunov exponents

<sup>148</sup> 0.3 to 5, Fig. 3a depicts that the dominant cases are period-1, period-2, and period-4, in the <sup>149</sup> ranges of  $\alpha$  from 0.3 to 0.671, 1.256 to 1.265, and 1.273 to 5 and the fixed point is seen <sup>150</sup> in the range from 0.672 to 1.255. Hopf bifurcation occurs at  $\alpha = 1.256$  where the chaos <sup>151</sup> behavior is noted during tiny range from 1.266 to 1.272 only. Figure 3b confirms the system <sup>152</sup> behavior shown in Fig. 3a, where the largest LEs are zero for the periodic solution in the <sup>153</sup> ranges  $0.3 \le \alpha \le 0, 671, 1, 256 \le \alpha \le 1.265, and 1.273 \le \alpha \le 5, all LEs are negative for$  $<sup>154</sup> the range of <math>0.672 \le \alpha \le 1.255$ , while one of LEs became positive for  $1.266 \le \alpha \le 1.272$ .

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Eigenvalues	$X^{e1}$	X <sup>e2</sup>
λ1	-7832.1	-7785.7 + 175.27 <i>i</i>
λ2	-3913.8 + 2913.86i	-7785.7 - 175.27i
λ3	-3913.8 - 2913.86i	-71.9
λ4	-0.487 + 0.064i	-38.644
λ5	-0.487 - 0.064i	14.707
λ6	-2.81	-5.125
λ7	-4.174	-0.468 + 0.047i
λ8	-5.322	-0.468 - 0.047i

**Table 3** The eigenvalues of the linearized system for  $K_{pd} = K_{pq} = 50$ ,  $K_{id} = K_{iq} = 100$ ,  $K_{p\omega} = 20$ ,  $K_{i\omega} = 106.4$ ,  $\psi_{dref} = 0.55$  Wb,  $\alpha = 1.3$ ,  $T_l = 3$  Nm and  $\omega_{ref} = 50$  rad/s,



**Fig. 4** IFOCIM drive system with  $K_{pd} = K_{pq} = 50$ ,  $K_{id} = K_{iq} = 100$ ,  $K_{p\omega} = 20$ ,  $\psi_{dref} = 0.55$  Wb,  $\alpha = 1.3$ ,  $\omega_{ref} = 50$  and  $T_L = 3$  Nm: **a** bifurcation diagram and the corresponding spectrum of the seven Lyapunov exponents **b**(i)  $L_1$ ,  $L_2$ ,  $L_3$ ,  $L_4$ ,  $L_5$ ,  $L_6$ ,  $L_7$  and the eighth Lyapunov exponent **b**(ii)  $L_8$  illustrate various behaviors of system with variation of  $K_{i\omega}$  upward in the range  $0 \le K_{i\omega} \le 120$ 

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**Fig. 5** Transient chaotic behavior with system parameters  $K_{pd} = K_{pq} = 50$ ,  $K_{id} = K_{iq} = 100$ ,  $K_{p\omega} = 20$ ,  $K_{i\omega} = 110$ ,  $\psi_{dref} = 0.55$  Wb,  $\alpha = 1.3$ ,  $\omega_{ref} = 50$  and  $T_L = 3$  Nm: **a** phase portrait projection  $(x_3, x_4)$  and the initial value  $(x_1(0), x_2(0), x_3(0), x_4(0), x_5(0), x_6(0), x_7(0), x_8(0)) = (0,0,-1.265,-0.5918,0,0,0)$  and **b** the corresponding time series of  $x_4$ 



**Fig. 6** Two-dimensional speed bifurcation diagram where the system parameters are  $K_{pd} = K_{pq} = 50$ ,  $K_{id} = K_{iq} = 100$ ,  $\psi_{dref} = 0.55$  Wb,  $\alpha = 1.3$ ,  $T_L = 3$  Nm and  $\omega_{ref} = 50$  rad/s

For  $K_{i\omega} = 90$ , Fig. 3c, d shows that the boundaries of the bifurcation regions are shifted and the chaotic domain is increased. The results show that the chaos occurs in a very small range of  $\alpha$ , while it is noted that the results in the previous studies [9–14, 16] showed that the general behavior of the system is the occurrence of SNB, HB, BTB, and ZHB.

As shown in Fig. 3, the value of  $\alpha$  which leads to chaos is varied in a small ranges around 1.27 for  $K_{i\omega} = 5$  and around 1.3 for  $K_{i\omega} = 90$ . Besides, in practical application upper limit value of  $\alpha$  is about 1.5 [18]. Therefore,  $\alpha = 1.3$  is selected to investigate the system dynamics due to the changes of the controller gain(s).

The system dynamics is verified numerically to investigate the bifurcation behavior due to  $K_{i\omega}$  change for a certain value of  $\alpha$  (= 1.3) as illustrated in Fig. 4a. It is noted that for  $K_{i\omega} = 0$ , a stable periodic solution occurs with period-2; period-doubling bifurcation route to chaos is appeared for  $K_{i\omega} \ge 0.1$ . The period-4 occurs for  $K_{i\omega}$  from 0.1 to 23, period-8 for  $K_{i\omega}$  from 23.1 to 28.3, and period-16 for  $K_{i\omega}$  from 28.4 to 29.7. The system exhibits chaotic for  $K_{i\omega}$  from 29.8 to 106.3, while period-5 and period-10 are also noted at a windows



**Fig. 7** Phase portrait projected  $(i_{qs}, i_{ds})$  in A with system parameters that are  $K_{pd} = K_{pq} = 50$ ,  $K_{id} = K_{iq} = 100$ ,  $K_{p\omega} = 20$ ,  $\psi_{dref} = 0.55$  Wb,  $\alpha = 1.3$ ;  $T_L = 3$  Nm and  $\omega_{ref} = 50$  rad/sec **a** for  $K_{i\omega} = 0$ , **b** for  $K_{i\omega} = 20$ , **c** for  $K_{i\omega} = 26$ , **d** for  $K_{i\omega} = 29$ , **e** for  $K_{i\omega} = 76$ , **f** for  $K_{i\omega} = 77$ , **g** for  $K_{i\omega} = 50$ , and **h** time series responses for direct currents  $(i_{ds})$  in A and rotor speed  $(\omega_r)$  in rad/sec for  $K_{i\omega} = 50$ 

 $K_{i\omega}$  from 75.6 to 76.7 and  $K_{i\omega}$  from 76.8 to 77.7. Also, there are windows for fixed-point 169 spread between the chaos region for  $K_{i\omega}$  from 104.3 to 104.6 and  $K_{i\omega}$  from 104.9 to 105. 170 For  $K_{i\omega} \ge 106.4$ ; the system tracks speed command perfectly which is noted as fixed point. 171 The Lyapunov exponents spectrum is obtained with respect to  $K_{i\omega}$  change. The simulation 172 results confirmed the bifurcation diagram. From Fig. 4b, the largest Lyapunov exponents spec-173 trum shows that the system has periodic behavior for  $K_{i\omega}$  from 0 to 29.7 and then the chaos 174 state has occurred for  $K_{i\omega}$  from 29.8 to 106.3. All the eight Lyapunov exponents are negative 175 for  $K_{i\omega} \ge 106.4$  which denote fixed-point state. From Fig. 4b, the system shows positive LE 176

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**Fig. 8** Basins of attractions with system parameters as in Fig. 4 with  $K_{p\omega} = 45$  and  $K_{i\omega}$  as mentioned in subfigures, where in **a**, **b**, and **c**  $x_3$  and  $x_4$  are varied with  $x_1(0) = 0, x_2(0) = 0, x_5(0) = 0, x_6(0) = 0, x_7(0) = 0$ , and  $x_8(0) = 0$ , **d**, **e**, and **f**  $x_6$  and  $x_7$  are varied with  $x_1(0) = 0, x_2(0) = 0, x_3(0) = 0, x_4(0) = 0, x_5(0) = 0$ , and  $x_8(0) = 0$ , fixed-point behavior (red) and periodic behavior (yellow)

in the fixed-point behavior region that means it has transient chaotic behavior followed by fixed-point steady-state response. Figure 5 states the system transient chaos, Fig. 5a illustrates the phase portrait for initial value  $(x_1(0), x_2(0), x_3(0), x_4(0), x_5(0), x_6(0), x_7(0), x_8(0)) =$ (0,0,-1.265,-0.5918,0,0,0,0), and Fig. 5b shows the corresponding time series.

The effect of change of speed controller gains ( $K_{p\omega}$  and  $K_{i\omega}$ ) has been investigated to 181 get the two-dimensional bifurcation diagram as shown in Fig. 6. The red zones denote the 182 fixed-point behavior, while the yellow, light green, and green zones denote quasi-periodic 183 behavior. The chaos zones are colored with light blue, blue, light purple, and purple. The 184 diversity of the colors is due to the strength of the chaotic behavior. It is noted that the fixed-185 point state has the largest area of the 2D diagram, while the chaos behavior has very small 186 area. The diagram simplifies the boundaries of each of  $K_{p\omega}$  and  $K_{i\omega}$  for the designer to be 187 used according to the application. 188

Figure 7 shows the phase portrait projected  $(i_{qs}, i_{ds})$  and the corresponding time response 189 with  $K_{pd} = K_{pq} = 50$ ,  $K_{id} = K_{iq} = 100$ ,  $K_{p\omega} = 20$ ,  $\psi_{dref} = 0.55$  Wb,  $\alpha = 1.3$ ; 190  $T_L = 3$  Nm and  $\omega_{ref} = 50$ . Figure 7a illustrates period-2 when  $K_{i\omega} = 0$ . Period-doubling 191 period-4, period-8, and period-16 are plotted at  $K_{i\omega} = 20, 26$ , and 29 as shown in Fig. 7b–d, 192 respectively. Period doubling from period-5 to period-10 is illustrated in Fig. 7e, f when 193  $K_{i\omega}$  equals 76 and 77, respectively. Chaotic behavior is represented in Fig. 7g at  $K_{i\omega} = 50$ , 194 while Fig. 7h represents the time series responses for direct currents  $(i_{ds})$  and rotor speed 195  $(\omega_r)$  at  $K_{i\omega} = 50$ . The figures emphasize the bifurcation diagrams and Lyapunov exponents 196 197 spectrum.

### 198 3.4 Basins of attractions

This subsection discusses the basins of attractions and multistability. The nonlinear systems 199 are sensitive to the changes in its parameters and the initial conditions of the state variables. 200 Some of the system variables' initial values have been used to discover the IFOC drive system 201 behavior. In Fig. 8, the system shows two different attractors: fixed point (red) and periodic 202 (yellow). Figure 8a-c represents different attractors with respect to the change in initial values 203 of  $x_3$  and  $x_4$  with  $K_{iw} = 10, 20, \text{ and } 40$ , respectively. The other variables have constant initial 204 values  $x_1(0) = 0$ ,  $x_2(0) = 0$ ,  $x_5(0) = 0$ ,  $x_6(0) = 0$ ,  $x_7(0) = 0$ , and  $x_8(0) = 0$ . As shown in 205 Fig. 8d–f, the initial values of  $x_1, x_2, x_3, x_4, x_5$ , and  $x_8$  have been adjusted to be 0, 0, 0, 0, 0, 206 0, and 0 for  $K_{iw} = 10, 20, \text{ and } 40$ , respectively, and the values of  $x_6(0), x_7(0)$  are changed. 207 Figure 8d–f displays fixed point and periodic attractors due to the changes in the initial values 208 of  $x_6$  and  $x_7$  for  $K_{iw} = 20$ . These different attractors, which are shown in Fig. 1, reveal that 209 the IFOCIM system is sensitive to the variation of the initial value of IFOC system variables. 210 From Figs. 4, 5, and 8, one can conclude that the IFOCIM model has multistability. 211

## 212 4 Conclusions

The full-order three-phase IM has been modeled in synchronous reference frame and con-213 trolled by using indirect field-oriented control method. The numerical analysis is used to 214 investigate the system behavior due to control parameters change. The variation of slip speed 215 compensator gain, integral gain, and proportional gain of speed loop controller are used to 216 test the system dynamics. The simulation results show interesting notes related to the gain 217 of the slip speed compensator bifurcation values where the chaos behavior is shown in very 218 small region which is difficult to be indicated compared with the dominant limit cycles solu-219 tions; while the quasi-periodic behavior has the largest region, the fixed-point state has been 220 noted in significant range of  $\alpha$ . Also, the results show that the system has been bifurcated 221 into period-2, period-4, period-8, period-16, and then the system becomes chaotic due to 222 integral gain variation of speed loop. The bifurcation diagram and Lyapunov exponent spec-223 trum confirm these situations. Period-5 and period-10 have been indicated in a window inside 224 the bifurcation diagram. The 2D bifurcation diagram gives visualization about the accepted 225 ranges for each of  $K_{p\omega}$  and  $K_{i\omega}$  to avoid the undesirable cases. Also, the system has mul-226 tistability for different initial values of the state variables. In future work, a suitable control 227 method will be used to suppress the chaos in the IFOC drive system. 228

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