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## Fe<sub>2</sub>MnSi<sub>x</sub>Ge<sub>1-x</sub>: influence thermoelectric properties of varying the germanium content

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The semi-classical Boltzmann theory, as implemented in the BoltzTraP code, was used to study the influence of varying the germanium content on the thermoelectric properties of the Heusler compounds, Fe<sub>2</sub>MnSi and Fe<sub>2</sub>MnGe. The electrical conductivity ( $\sigma/\tau$ ), the Seebeck coefficient ( $S$ ), the electronic power factor ( $S^2\sigma$ ), the electronic thermal conductivity ( $\kappa_e$ ), the electronic heat capacity  $c_{el}(T_{el})$ , and the Hall coefficient ( $R_H$ ), as a function of temperature at certain values of chemical potential ( $\mu$ ) with constant relaxation time ( $\tau$ ), were evaluated on the basis of the calculated band structure using the standard Boltzmann kinetic transport theory and the rigid band approach. The increase/reduction in the electrical conductivity ( $\sigma = ne\mu$ ) of Fe<sub>2</sub>MnSi<sub>x</sub>Ge<sub>1-x</sub> alloys is attributed to the density of charge carriers ( $n$ ) and their mobility ( $\mu = e\tau/m_e$ ). The  $S$  for Fe<sub>2</sub>MnGe is negative over the entire temperature range, which represents the n-type concentration. Whereas Fe<sub>2</sub>MnSi shows a positive  $S$  up to 250 K and then drops to negative values, which confirms the existence of the p-type concentration between 100–250 K. Fe<sub>2</sub>MnSi<sub>0.25</sub>Ge<sub>0.75</sub>/Fe<sub>2</sub>MnSi<sub>0.5</sub>Ge<sub>0.5</sub>/Fe<sub>2</sub>MnSi<sub>0.75</sub>Ge<sub>0.25</sub> possess positive  $S$  up to 270/230/320 K and then drop to negative values. The power factor of Fe<sub>2</sub>MnGe rapidly increases with increasing temperature, while for Fe<sub>2</sub>MnSi it is zero up to 300 K, and then rapidly increases with increasing temperature. The  $S^2\sigma$  of Fe<sub>2</sub>MnSi<sub>0.25</sub>Ge<sub>0.75</sub> is zero between 250–350 K, whereas Fe<sub>2</sub>MnSi<sub>0.5</sub>Ge<sub>0.5</sub> possesses a zero  $S^2\sigma$  of up to 320 K. Fe<sub>2</sub>MnSi<sub>0.75</sub>Ge<sub>0.25</sub> has a zero  $S^2\sigma$  between 200 and 500 K. The electronic thermal conductivity ( $\kappa_e$ ) and the electronic heat capacity  $c_{el}(T_{el})$  increases with increasing temperature. The parent compounds (Fe<sub>2</sub>MnGe and Fe<sub>2</sub>MnSi) show the highest positive value of the Hall coefficient  $R_H$  at 100 K, and then drop to negative values at 260 K. On the other hand, the  $R_H$  for Fe<sub>2</sub>MnSi<sub>0.25</sub>Ge<sub>0.75</sub>, Fe<sub>2</sub>MnSi<sub>0.5</sub>Ge<sub>0.5</sub> and Fe<sub>2</sub>MnSi<sub>0.75</sub>Ge<sub>0.25</sub> alloys exhibit negative  $R_H$  along the temperature scale. The behavior of  $R_H$  is attributed to the concentration of the charge carriers and their mobility.

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### 1. Introduction

Half metallic compounds have received a significant amount of attention<sup>1–13</sup> because of the spin degree of freedom in electronics.<sup>14–17</sup> Significant effort has been paid to understanding the mechanism behind half-metallic magnetism and to study its implications on various physical properties.<sup>18,19</sup> The field of spin-based electronics (spintronics) aims to exploit a large class of emerging materials, such as ferromagnetic semiconductors,<sup>20,21</sup> high temperature superconductors,<sup>22</sup> organic ferromagnets,<sup>23,24</sup> organic semiconductors,<sup>25</sup> and carbon nanotubes<sup>26,27</sup> based devices to bring novel functionalities to traditional devices. In other areas within spintronics, as high as possible a degree of spin polarisation is required, for which half metals are considered the best options. Half-metallic compounds behave as

metals in one spin direction, and behave as semiconductors or insulators in the opposite spin direction.

In 1983, De Groot *et al.*<sup>28,29</sup> discovered the half-metallic ferromagnetic (HMF). Ever since this discovery, extensive studies have been carried out and many HMF compounds have been theoretically predicted, and some of them experimentally confirmed.<sup>30–32</sup> It is well known that the most important candidates for 100% spin polarization are semi-Heusler alloys,<sup>19,28,29,33–35</sup> zinc-blende structured materials,<sup>36,37</sup> semi-metallic magnetic oxides CrO<sub>2</sub> and Fe<sub>3</sub>O<sub>4</sub>,<sup>11,38,39</sup> and full Heusler alloys.<sup>9,40</sup> Fe<sub>2</sub>MnSi<sub>1-x</sub>Ge<sub>x</sub> alloys are considered as very interesting HMF materials.<sup>41–43</sup> Fe<sub>2</sub>MnSi<sub>1-x</sub>Ge<sub>x</sub> alloys can be successfully applied to highly efficient spin injection and detection through Schottky tunnel barriers in group-IV semiconductor devices.

Epitaxial Fe<sub>2</sub>MnSi thin films have a Curie temperature of about 210 K, which is much lower than room temperature;<sup>44</sup> however, only limited experimental work has been done on these materials. Zhang *et al.* have studied Fe<sub>2</sub>MnSi<sub>1-x</sub>Ge<sub>x</sub> alloys and found there is no significant change in the Curie temperature and the spontaneous magnetization, with change the Ge content in the single-phase L2<sub>1</sub> compounds. There is no field-

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induced transition and the magneto-caloric effect is rather small throughout the  $\text{Fe}_2\text{MnSi}_{1-x}\text{Ge}_x$  series.<sup>45</sup> In addition, in the  $L2_1$ -type structure, both  $\text{Fe}_2\text{MnGe}$  and  $\text{Fe}_2\text{MnSi}$  have a Curie temperature of around 250 K.<sup>45</sup> Therefore, it is worth studying the transport properties of  $\text{Fe}_2\text{MnSi}_x\text{Ge}_{1-x}$  alloys by varying the germanium content between 0.0 and 1.0, in steps of 0.25 atoms.

The rest of the paper is organized as; the structural aspects and the computational details are presented in Section 2. The results and discussion are demonstrated in Section 3. Section 4 summarizes the results.

## 2. Structural aspects and computational details

To study the influence of varying the germanium content on the thermoelectric properties of the Heusler compounds  $\text{Fe}_2\text{MnSi}$  and  $\text{Fe}_2\text{MnGe}$ , the semi-classical Boltzmann theory as implemented in the BoltzTraP code<sup>46</sup> was used. The thermoelectric transport tensors can be evaluated on the basis of the calculated band structure using the standard Boltzmann kinetic transport theory and the rigid band approach.<sup>47</sup> The electrical conductivity  $\sigma_{\alpha\beta}$ , the Seebeck coefficient  $S_{\alpha\beta}$ , and the electronic thermal conductivity  $k_{\alpha\beta}^0$  tensors are the main transport properties.

In this work, the germanium content in  $\text{Fe}_2\text{MnSi}_x\text{Ge}_{1-x}$  alloys was varied between 0.0 and 1.0, in steps of 0.25 atoms. The parent compounds crystallize in the  $L2_1$  structure, which consists of four face-centered cubic sublattices with space  $Fm\bar{3}m$ . The  $L2_1$  phase is a cubic superstructure of four interpenetrating fcc sublattices, A, B, C, and D, centered at (0 0 0), (1/4 1/4 1/4), (1/2 1/2 1/2), and (3/4 3/4 3/4). Each A atom is at the center of a cube of four B atoms and four D atoms (Fig. 1). To trace the variation in the composition, we employed the supercell approach. The electronic structure was calculated using the full potential linear augmented plane wave, plus the local orbitals method, as implemented in WIEN2k code<sup>48</sup> with the Engel–Vosko generalized gradient approximation for the exchange–correlation potential. The structures were fully relaxed by minimizing the forces acting on each atom. A mesh of 5000  $k$ -points in the irreducible Brillouin zone (IBZ) for binary, as well as for ternary alloys, was used for calculating the thermoelectric properties. The  $K_{\text{max}}$  was set at  $9.0/R_{\text{MT}}$  and made the expansion up to  $l = 10$  in the muffin tins spheres. The convergence of the total energy in the self-consistent calculations was taken with respect to the total charge of the system with a tolerance 0.0001 electron charges.

## 3. Results and discussion

### 3.1. Salient features of the electronic band structures

The calculated electronic band structure of  $\text{Fe}_2\text{MnSi}_x\text{Ge}_{1-x}$  ( $x = 0.0, 0.25, 0.5, 0.75, 1.0$ ) alloys along the high symmetry point in the first BZ are represented in Fig. 2a–e. These figures suggest that the investigated alloys are metallic, as it is clear that there exists some bands that controlled the overlapping around the Fermi energy ( $E_F$ ). The density of states at  $E_F$  is determined by the overlap between the valence and conduction

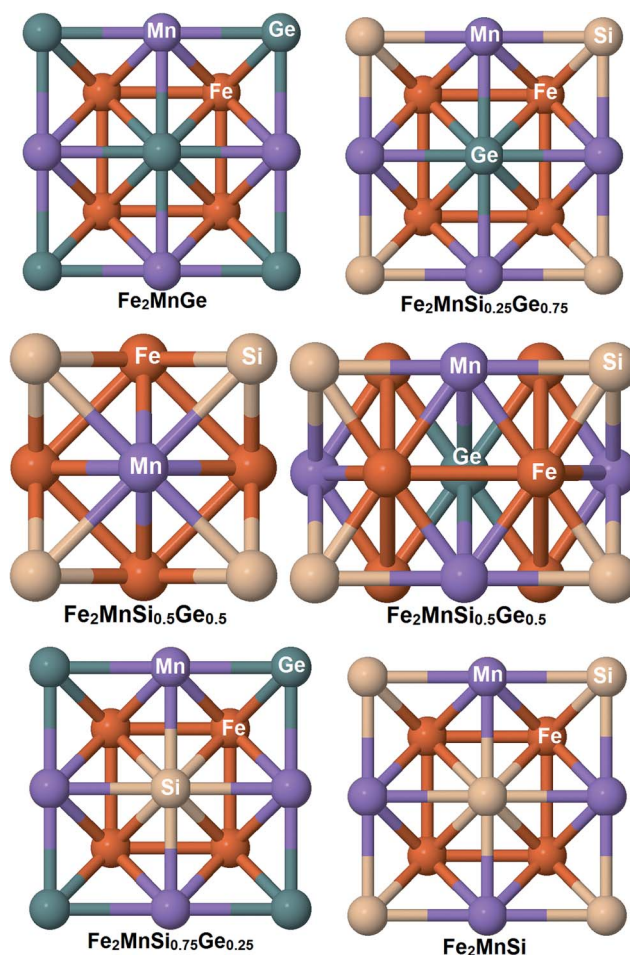


Fig. 1 Structure of the unit cell of  $\text{Fe}_2\text{MnSi}_x\text{Ge}_{1-x}$  ( $x = 0.0, 0.25, 0.5, 0.75$  and  $1.0$ ) alloys.

bands. This overlap is strong enough, indicating a metallic origin with different values of DOS at  $E_F$ ,  $N(E_F)$  (Table 1). The electronic specific heat coefficient ( $\gamma$ ), which is function of the density of states, can be calculated using the expression,  $\gamma = \frac{1}{3}\pi^2 N(E_F)k_B^2$ , where  $N(E_F)$  is the density of states at  $E_F$ , and  $k_B$  is the Boltzmann constant. The calculated density of states at the Fermi energy  $N(E_F)$  enables us to calculate the bare electronic specific heat coefficient (Table 1). It is clear that substituting 0.25 Ge atoms by Si atoms leads to increasing the metallic nature of  $\text{Fe}_2\text{MnSi}_{0.25}\text{Ge}_{0.75}$  by 3.7% with respect to  $\text{Fe}_2\text{MnGe}$ , while substituting 0.5 Ge atoms by Si atoms causes an increase in the metallic nature of  $\text{Fe}_2\text{MnSi}_{0.5}\text{Ge}_{0.5}$  by 1.9% with respect to  $\text{Fe}_2\text{MnGe}$ . Further increasing the content of Si atoms leads to increasing the metallic nature of  $\text{Fe}_2\text{MnSi}_{0.75}\text{Ge}_{0.25}$  by 3% with respect to  $\text{Fe}_2\text{MnGe}$ , and finally substituting Ge by Si causes a reduction of the metallic nature of  $\text{Fe}_2\text{MnSi}$  by 0.9% with respect to  $\text{Fe}_2\text{MnGe}$ . The same trends were observed for the electronic specific heat coefficient ( $\gamma$ ).

### 3.2. Transport properties

Fig. 3a illustrates the influence of substituting Ge by Si (in steps of 0.25 atoms) on the electrical conductivity ( $\sigma/\tau$ ) of the Heusler

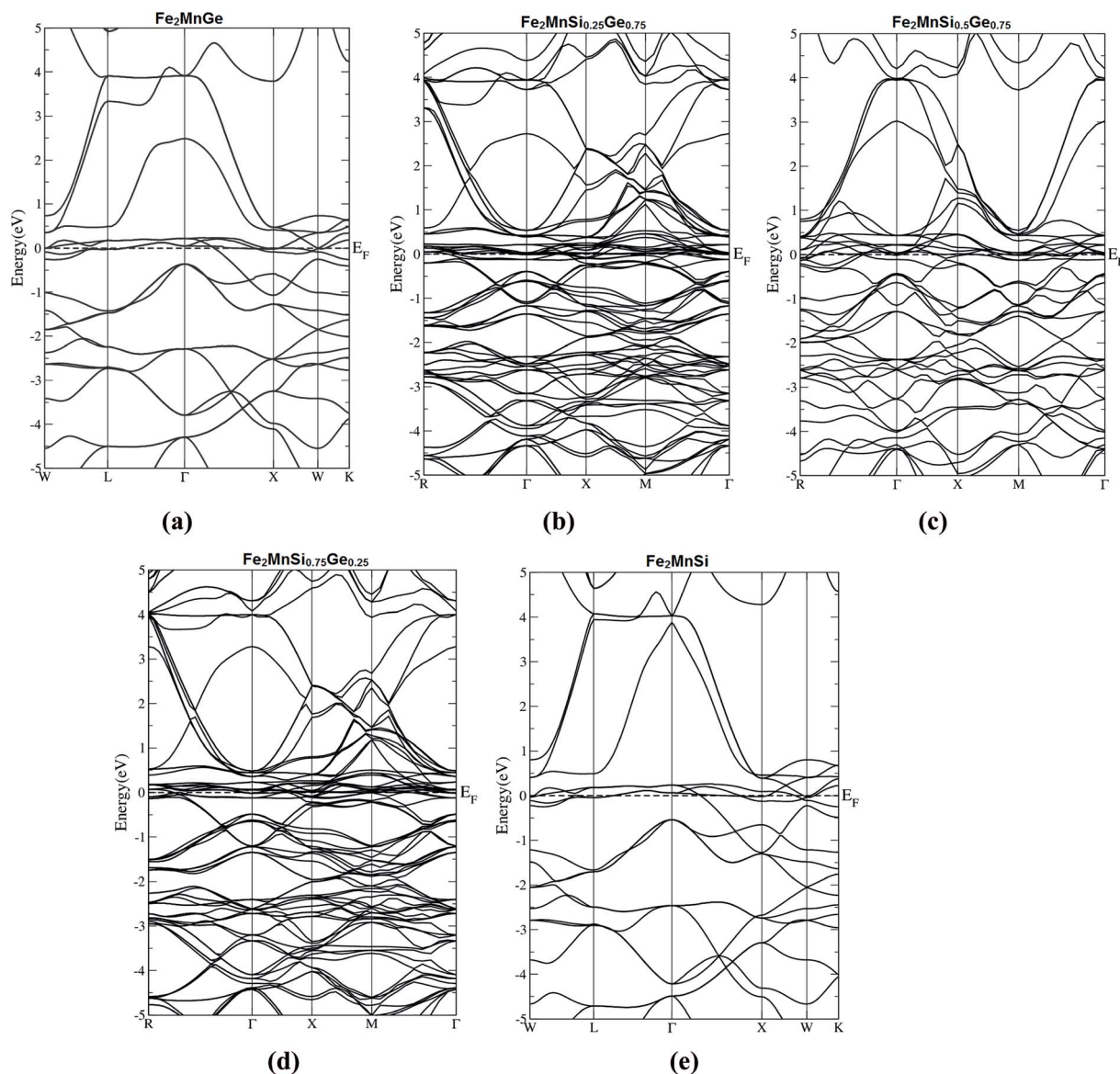


Fig. 2 (a–e) Calculated electronic band structure of  $\text{Fe}_2\text{MnSi}_x\text{Ge}_{1-x}$  ( $x = 0.0, 0.25, 0.5, 0.75$  and  $1.0$ ) alloys.

compounds  $\text{Fe}_2\text{MnGe}$  and  $\text{Fe}_2\text{MnSi}$ . In all cases, we notice that  $\sigma/\tau$  increases with temperature, and it is clear that the increasing rate is dependent on the concentration of Ge and Si atoms. The end compounds ( $\text{Fe}_2\text{MnGe}$  and  $\text{Fe}_2\text{MnSi}$ ) show the highest value for  $\text{Fe}_2\text{MnSi}$  of about  $1.49 \times 10^{20} (\Omega \text{ ms})^{-1}$  at 100 K and  $1.9 \times 10^{20} (\Omega \text{ ms})^{-1}$  at 800 K; while for  $\text{Fe}_2\text{MnGe}$ , it is  $1.4 \times 10^{20} (\Omega \text{ ms})^{-1}$  at 100 K and  $1.82 \times 10^{20} (\Omega \text{ ms})^{-1}$  at 800 K. With substituting 0.25 Ge by Si ( $\text{Fe}_2\text{MnSi}_{0.25}\text{Ge}_{0.75}$ ), we notice that the value of  $\sigma/\tau$  drops to the lowest values along the whole

temperature range. Then, increasing the content of Si atoms to be equal to Ge atoms ( $\text{Fe}_2\text{MnSi}_{0.5}\text{Ge}_{0.5}$ ) causes an increase in the electrical conductivity to its maximum value of about  $1.1 \times 10^{20} (\Omega \text{ ms})^{-1}$  at 100 K and  $1.4 \times 10^{20} (\Omega \text{ ms})^{-1}$  at 800 K. Further increasing the content of Si atoms ( $\text{Fe}_2\text{MnSi}_{0.75}\text{Ge}_{0.25}$ ) leads to a reduction in the electrical conductivity to  $0.9 \times 10^{20} (\Omega \text{ ms})^{-1}$  at 100 K and  $1.3 \times 10^{20} (\Omega \text{ ms})^{-1}$  at 800 K. From above, we can conclude that the increase/reduction in the electrical conductivity of  $\text{Fe}_2\text{MnSi}_x\text{Ge}_{1-x}$  alloys is attributed to the density of

Table 1 Density of states at Fermi energy  $N(E_F)$  states per eV cell and bare electronic specific heat coefficient  $\gamma$  ( $\text{mJ mol}^{-1} \text{K}^{-2}$ ) of  $\text{Fe}_2\text{MnSi}_x\text{Ge}_{1-x}$  ( $x = 0.0, 0.25, 0.5, 0.75, 1.0$ ) alloys

	$\text{Fe}_2\text{MnGe}$	$\text{Fe}_2\text{MnSi}_{0.25}\text{Ge}_{0.75}$	$\text{Fe}_2\text{MnSi}_{0.5}\text{Ge}_{0.5}$	$\text{Fe}_2\text{MnSi}_{0.75}\text{Ge}_{0.25}$	$\text{Fe}_2\text{MnSi}$
$N(E_F)$ states per eV cell	17.11	65.0	33.93	58.15	16.07
$\gamma$ ( $\text{mJ mol}^{-1} \text{K}^{-2}$ )	2.96	11.27	5.88	10.08	2.78

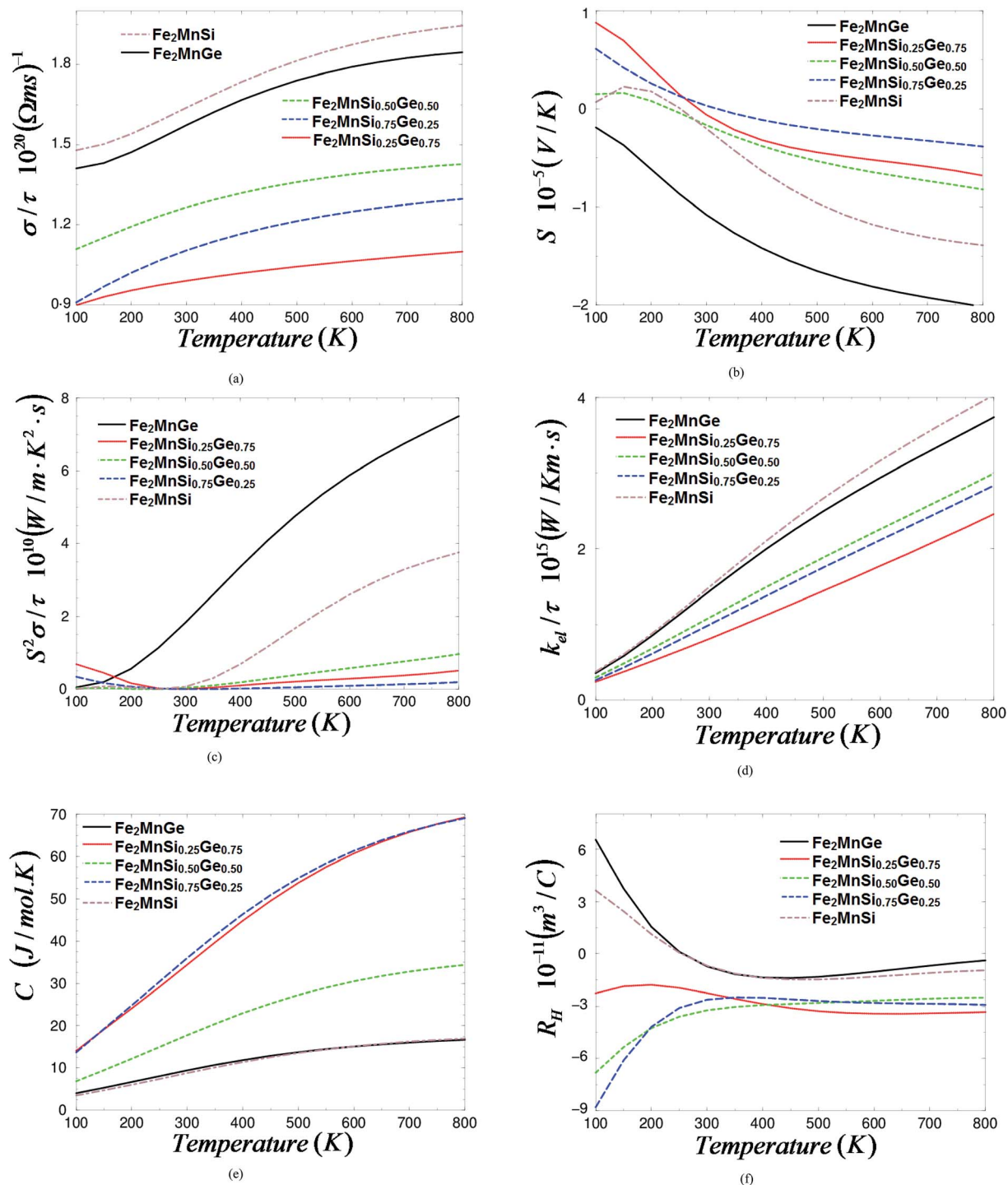


Fig. 3 (a) Calculated electrical conductivity; (b) calculated Seebeck coefficient; (c) calculated power factor; (d) calculated electronic thermal conductivity; (e) calculated electronic heat capacity; (f) calculated Hall coefficient.

charge carriers ( $n$ ) and their mobility ( $\mu = e\tau/m_e$ ), since the electrical conductivity ( $\sigma = ne\mu$ ) is related to the density of charge carriers and their mobility.

The Seebeck coefficient  $S_{\alpha\beta}$  and the electrical conductivity  $\sigma_{\alpha\beta}$  tensors can be written as:<sup>47,49</sup>

$$S_{\alpha\beta}(T; \mu) = \frac{1}{eTQ\sigma_{\alpha\beta}(T; \mu)} \int \sigma_{\alpha\beta}(\epsilon)(\epsilon - \mu) \times \left[ -\frac{\partial f_{\mu}(T; \epsilon)}{\partial \epsilon} \right] d\epsilon$$

$$\sigma_{\alpha\beta}(T; \mu) = \frac{1}{Q} \int \sigma_{\alpha\beta}(\epsilon) \left[ -\frac{\partial f_{\mu}(T; \epsilon)}{\partial \epsilon} \right] d\epsilon$$

From the above formulas, it is clear that the Seebeck coefficient is inversely proportional to the electrical conductivity, and that these quantities are functions of temperature ( $T$ ) and chemical potential ( $\mu$ ).<sup>47,49</sup>

Fig. 3b illustrates the Seebeck coefficient ( $S$ ) as a function of temperature at certain values of chemical potential ( $\mu$ ). Following Fig. 3b, one can see that the  $S$  for  $\text{Fe}_2\text{MnGe}$  is negative over the entire temperature range, which represents the n-type concentration. It is clear that  $S$  reduces rapidly with increasing the temperature, and it possesses a maximum value at 100 K ( $-0.2 \times 10^{-5} \text{ V K}^{-1}$ ) and the lowest value at 800 K. Whereas,  $\text{Fe}_2\text{MnSi}$  shows positive  $S$  up to 250 K, and then drop to negative values, which confirms the existence of the p-type concentration between 100 K and 250 K. When we substitute 0.25 Ge atoms by Si ( $\text{Fe}_2\text{MnSi}_{0.25}\text{Ge}_{0.75}$ ), we notice that the Seebeck coefficient shows the maximum positive value at 100 K ( $0.9 \times 10^{-5} \text{ V K}^{-1}$ ), and then reduces with increasing the temperature up to 270 K. Above this temperature,  $S$  drops to negative values, to reach the lower value of about ( $-0.7 \times 10^{-5} \text{ V K}^{-1}$ ) at 800 K.

With substituting half the content of Ge atoms by the same content of Si atoms ( $\text{Fe}_2\text{MnSi}_{0.5}\text{Ge}_{0.5}$ ), we notice that the Seebeck coefficient reduced, to show a maximum value at 100 K of about ( $0.2 \times 10^{-5} \text{ V K}^{-1}$ ), and then drops to negative values at 230 K to reach  $-0.8 \times 10^{-5} \text{ V K}^{-1}$  at 800 K. In further increasing the Si content at the cost of the Ge content ( $\text{Fe}_2\text{MnSi}_{0.75}\text{Ge}_{0.25}$ ), the value of the Seebeck coefficient at 100 K increases to  $0.6 \times 10^{-5} \text{ V K}^{-1}$  with respect to the value of  $S$  obtained for  $\text{Fe}_2\text{MnSi}_{0.5}\text{Ge}_{0.5}$ , and then drops to negative values at 320 K.

Fig. 3c shows the electronic power factor ( $S^2\sigma$ ) versus the temperature at certain values of chemical potential ( $\mu$ ) and constant relaxation time ( $\tau$ ). We notice that the power factor of  $\text{Fe}_2\text{MnGe}$  rapidly increases with increasing the temperature, to reach the maximum value ( $9 \times 10^{10} \text{ W m}^{-1} \text{ K}^{-2} \text{ s}^{-1}$ ) at 800 K. While for  $\text{Fe}_2\text{MnSi}$ , the power factor is zero up to 300 K, and then rapidly increases with increasing temperature to reach the maximum value ( $3.9 \times 10^{10} \text{ W m}^{-1} \text{ K}^{-2} \text{ s}^{-1}$ ) at 800 K. With replacing 0.25 Ge atoms by Si ( $\text{Fe}_2\text{MnSi}_{0.25}\text{Ge}_{0.75}$ ), the power factor increases with respect to all other concentrations, and shows its maximum value of about ( $0.8 \times 10^{10} \text{ W m}^{-1} \text{ K}^{-2} \text{ s}^{-1}$ ) at 100 K, and then reduces with increasing temperature to reach a zero value of  $S^2\sigma$  between 250 K and 350 K. Above this temperature range,  $S^2\sigma$  increases with increasing temperature, to reach  $0.2 \times 10^{10} \text{ W m}^{-1} \text{ K}^{-2} \text{ s}^{-1}$  at 800 K. Substituting 0.5 of Ge atoms by Si ( $\text{Fe}_2\text{MnSi}_{0.5}\text{Ge}_{0.5}$ ) causes the power factor to drop to zero up to 320 K. Then above 350 K, the power factor increases with increasing temperature, to reach  $1.0 \times 10^{10} \text{ W m}^{-1} \text{ K}^{-2} \text{ s}^{-1}$  at 800 K. In the last case ( $\text{Fe}_2\text{MnSi}_{0.75}\text{Ge}_{0.25}$ ), when we reduced the content of Ge to 0.25, the power factor became  $0.4 \times 10^{10} \text{ W m}^{-1} \text{ K}^{-2} \text{ s}^{-1}$  at 100 K, and then dropped to zero between 200 K and 500 K, while above 500 K, the Seebeck coefficient showed an insignificant increase to reach  $0.2 \times 10^{10} \text{ W m}^{-1} \text{ K}^{-2} \text{ s}^{-1}$  at 800 K.

The electronic thermal conductivity ( $\kappa_e$ ) can be estimated from the electrical conductivity ( $\sigma$ ) using Wiedemann–Franz's law. Fig. 3d illustrate  $\kappa_e$  for  $\text{Fe}_2\text{MnSi}_x\text{Ge}_{1-x}$  alloys as a function of temperature at certain values of chemical potential. We notice that for all  $\text{Fe}_2\text{MnSi}_x\text{Ge}_{1-x}$  alloys,  $\kappa_e$  increases rapidly with increasing temperature. The end compound  $\text{Fe}_2\text{MnSi}$  shows the

highest value of  $\kappa_e$  between 100 K and 800 K. While  $\kappa_e$  for  $\text{Fe}_2\text{MnGe}$  lies directly below that of  $\text{Fe}_2\text{MnSi}$  exhibiting the same trend. When we replace a quarter of the Ge atoms by Si ( $\text{Fe}_2\text{MnSi}_{0.25}\text{Ge}_{0.75}$ ), the thermal conductivity drops down to the lowest value along the temperature scale. With increasing the content of Si atoms to be equal to that of Ge atoms ( $\text{Fe}_2\text{MnSi}_{0.5}\text{Ge}_{0.5}$ ), we can see that the  $\kappa_e$  values increases along the temperature scale. Substituting more Ge atoms by Si atoms ( $\text{Fe}_2\text{MnSi}_{0.75}\text{Ge}_{0.25}$ ) leads to a reduction in the values of the electronic thermal conductivity with respect to that of  $\text{Fe}_2\text{MnSi}_{0.5}\text{Ge}_{0.5}$ . Following Fig. 3d, we can conclude that the electronic thermal conductivity is very sensitive to the density of the charge carriers and their mobility. The thermal conductivity has contributions from the lattice and electrons, but BoltzTraP calculates only the electronic part. In the absence of any calculations or measurements of the lattice thermal conductivity, it is difficult to confirm which alloy will have the largest figure of merit (FOM).

The electronic heat capacities  $c_{\text{el}}(T_{\text{el}})$  for  $\text{Fe}_2\text{MnSi}_x\text{Ge}_{1-x}$  alloys as a function of temperature at certain values of chemical potential with constant relaxation time are plotted in Fig. 3e. Here, we consider only the electronic contribution to the specific heat, because there is a linear relationship between the electronic specific heat and temperature *i.e.*,  $c_{\text{el}}(T_{\text{el}}) = \gamma T_{\text{el}}$ , where  $\gamma$  = the Sommerfeld coefficient.<sup>50,51</sup> The electrons are excited to the upper empty space and there is a smearing of Fermi below the Fermi level, which together contribute to the heat capacity. From Fig. 3e, we can see that the heat capacity for the end compounds ( $\text{Fe}_2\text{MnGe}$  and  $\text{Fe}_2\text{MnSi}$ ) slowly increases with temperature up to 500 K, and then reach saturation up to 800 K.  $\text{Fe}_2\text{MnSi}_{0.25}\text{Ge}_{0.75}$  alloy shows higher values of  $c_{\text{el}}(T_{\text{el}})$  compared to the parents. Increasing the Si content ( $\text{Fe}_2\text{MnSi}_{0.5}\text{Ge}_{0.5}$ ) causes a reduction in the  $c_{\text{el}}(T_{\text{el}})$  lower than that of  $\text{Fe}_2\text{MnSi}_{0.25}\text{Ge}_{0.75}$  but higher than that of the parents. Further increasing the Si content ( $\text{Fe}_2\text{MnSi}_{0.75}\text{Ge}_{0.25}$ ) causes an increase in  $c_{\text{el}}(T_{\text{el}})$ , showing the highest value among the others. It is clear from Fig. 3e that the electronic heat capacity of  $\text{Fe}_2\text{MnSi}_x\text{Ge}_{1-x}$  alloys obey the Debye approximation ( $T^3$ ), also called the “anharmonic approximation”.<sup>52</sup>

Fig. 3f presents the Hall coefficient  $R_{\text{H}}$  as a function of temperature; its value depends on the type, number, and properties of the charge carriers that constitute the current. It is clear that the parents compounds ( $\text{Fe}_2\text{MnGe}$  and  $\text{Fe}_2\text{MnSi}$ ) show the highest positive value of  $R_{\text{H}}$  at 100 K, which then rapidly reduces with increasing temperature to cross the zero line and then reach negative values at 260 K. Above 360 K, the  $R_{\text{H}}$  for the parents compounds is almost saturated. The  $R_{\text{H}}$  for  $\text{Fe}_2\text{MnSi}_{0.25}\text{Ge}_{0.75}$ ,  $\text{Fe}_2\text{MnSi}_{0.5}\text{Ge}_{0.5}$  and  $\text{Fe}_2\text{MnSi}_{0.75}\text{Ge}_{0.25}$  alloys exhibits negative  $R_{\text{H}}$  along the temperature scale, which is attributed to the concentration of the charge carriers and their mobility.

To the best of our knowledge, there are no previous experimental data or theoretical results for the thermoelectric properties of the investigated materials available in literature to make a meaningful comparison. We would like to mention here that in our previous works<sup>53–59</sup> we calculated the band gap, bond lengths, bond angles, and linear and nonlinear optical susceptibilities using the FPLAPW method on several systems whose energy band gap, bond lengths, bond angles, and linear

and nonlinear optical susceptibilities are known experimentally. We achieved very good agreement with the experimental data. Thus, we believe that our calculations reported in this paper could produce very accurate and reliable results, which therefore confirms the accuracy of the method used.

## 4. Conclusions

The full potential linear augmented plane wave plus local orbitals method, as implemented in WIEN2k code with the Engel–Vosko generalized gradient approximation for the exchange–correlation potential, were used to calculate band structure for  $\text{Fe}_2\text{MnSi}_x\text{Ge}_{1-x}$  ( $x = 0.0, 0.25, 0.5, 0.75$  and  $1.0$ ) alloys. Based on the calculated band structure, the semi-classical Boltzmann theory as implemented in the BoltzTraP code was used to study the influence of varying the germanium content on the thermoelectric properties of  $\text{Fe}_2\text{MnSi}_x\text{Ge}_{1-x}$  alloys as a function of temperature at certain values of chemical potential ( $\mu$ ) with a constant relaxation time ( $\tau$ ). The increase/reduction in the electrical conductivity ( $\sigma = ne\mu$ ) of  $\text{Fe}_2\text{MnSi}_x\text{Ge}_{1-x}$  alloys is attributed to the density of charge carriers ( $n$ ) and their mobility ( $\mu = e\tau/m_e$ ). The parent  $\text{Fe}_2\text{MnGe}$  compound exhibits negative  $S$  over the entire temperature range, which confirms the existence of an n-type carrier. While  $\text{Fe}_2\text{MnSi}$  shows positive  $S$  up to 250 K, and then drops to negative values, to represent the p-type charge carrier between 100 K and 250 K. The alloys  $\text{Fe}_2\text{MnSi}_{0.25}\text{Ge}_{0.75}/\text{Fe}_2\text{MnSi}_{0.5}\text{Ge}_{0.5}/\text{Fe}_2\text{MnSi}_{0.75}\text{Ge}_{0.25}$  all possess positive  $S$  up to 270/230/320 K. Above these temperatures, the Seebeck coefficient exhibits negative values. The power factor of  $\text{Fe}_2\text{MnGe}$  rapidly increases with increasing temperature, while for  $\text{Fe}_2\text{MnSi}$  it is zero up to 300 K, and then rapidly increases with increasing temperature.  $\text{Fe}_2\text{MnSi}_{0.25}\text{Ge}_{0.75}$  has a zero power factor between 250 K and 350 K. While  $\text{Fe}_2\text{MnSi}_{0.5}\text{Ge}_{0.5}$  shows a zero power factor up to 320 K. The  $\text{Fe}_2\text{MnSi}_{0.75}\text{Ge}_{0.25}$  alloy shows a zero power factor between 200 K and 500 K. The electronic thermal conductivity ( $\kappa_e$ ) and the electronic heat capacity  $c_{ei}(T_{ei})$  increase with increasing temperature. The parent compounds show the highest positive value of  $R_H$  at 100 K, and then drop to negative values at 260 K. The alloys  $\text{Fe}_2\text{MnSi}_{0.25}\text{Ge}_{0.75}$ ,  $\text{Fe}_2\text{MnSi}_{0.5}\text{Ge}_{0.5}$  and  $\text{Fe}_2\text{MnSi}_{0.75}\text{Ge}_{0.25}$  alloys exhibit negative  $R_H$  along the temperature scale. The positive and negative behavior of  $R_H$  is attributed to the concentration of the charge carriers and their mobility.

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