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# Specific features of electronic structures and optical susceptibilities of molybdenum oxide<sup>†</sup>

A. H. Reshak<sup>\*ab</sup>

Orthorhombic molybdenum trioxide,  $\alpha$ -MoO<sub>3</sub>, is comprehensively investigated using density function theory based on the all-electron full potential linear augmented plane wave (FPLAPW) method as implemented in the WIEN2k code within four types of exchange correlation potentials, namely, the local density approximation (CA-LDA), generalized gradient approximation (PBE-GGA), Engel-Vosko generalized gradient approximation (EVGGA) and the modified Becke-Johnson potential (mBJ). The conduction band minimum (CBM) is situated at  $\Gamma$  point of Brillouin zone (BZ), whereas the valence band maximum (VBM) is located at T point of BZ. Calculation demonstrated that  $\alpha$ -MoO<sub>3</sub> is an indirect band gap insulator. The calculated electronic band structure and the total density of states confirm that mBJ brings the calculated energy band gap (2.81 eV) closer to the experimental one (3.03, 3.10 eV). The electronic space charge density distribution of  $\alpha$ -MoO<sub>3</sub> is explored in two crystallographic planes, namely, (0 0 1) and (1 0 1), to scrutinize the origin of chemical bonds. It is found that the majority of the charges are accumulated on the O site and the distribution of electronic charge is spherical. The optical properties are calculated for three tensor components along the polarization directions [1 0 0], [0 1 0] and [0 0 1] with respect to the crystalline axes. It is found that the regions confined between 6.5 and 8.0 eV and 10.0 and 13.5 eV are considered as lossless regions. The calculated optical properties support our observation from the calculated electronic band structure and the density of states, which shows that LDA, GGA and EVGGA underestimate the energy band gap, while mBJ succeeds by a large amount in bringing the calculated energy band gap closer to the experimental one.

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## 1. Introduction

Recent studies confirm that transition metal oxides such as molybdenum trioxide ( $MoO_3$ ) have attracted great interest due to their excellent chemical and physical properties.  $MoO_3$  is useful for numerous applications<sup>1–5</sup> in electrochromic display devices, optical memories, as a cathode material in the development of high-energy density solid-state microbatteries, gas sensors and lithium batteries due to its wide range of stoichiometries and interesting behavior, which includes chromogenic and catalytic properties. The main application of molybdenum trioxide is as a raw material for the production of molybdenum metal and as an oxidation catalyst. Moreover, it is used as an additive in steel and other corrosion-resistant alloys, as an industrial catalyst, a pigment, a crop nutrient, a component of glass, a flame retardant for polyester and polyvinyl chloride resins, chemical reagent and

<sup>b</sup>Center of Excellence Geopolymer and Green Technology, School of Material Engineering, University Malaysia Perlis, 01007 Kangar, Perlis, Malaysia in ceramics and enamels. Therefore, molybdenum trioxide has many scientific and technological applications.  $MoO_3$  is a  $4d^0Mo(v_1)$  compound, and it is decomposed into other molybdenum oxide compounds.<sup>6</sup>  $\alpha$ -MoO<sub>3</sub> is an insulator with a band gap of 3.1 eV.<sup>6</sup> Klinbumrung *et al.*<sup>7</sup> produced orthorhombic  $\alpha$ -MoO<sub>3</sub> microplates from  $(NH_4)_6Mo_7O_{24} \cdot 4H_2O$  solid powder using a 900 W microwave plasma for 40, 50, and 60 min. They reported that  $\alpha$ -MoO<sub>3</sub> is a wide bandgap n-type semiconductor.

Molybdenum trioxide exists in orthorhombic structure  $\alpha$ -MoO<sub>3</sub> (thermodynamically stable),<sup>8,9</sup> monoclinic structure  $\beta$ -MoO<sub>3</sub> (metastable),<sup>10</sup> high pressure monoclinic structure MoO<sub>3</sub>-II<sup>11</sup> and hexagonal structure h-MoO<sub>3</sub>.<sup>12,13</sup>  $\alpha$ -MoO<sub>3</sub> is the most stable phase at the normal conditions.<sup>8,9</sup> Atuchin *et al.*<sup>14</sup> have grown high-quality platelet  $\alpha$ -MoO<sub>3</sub> single crystals with dimensions of 1000 × 200 × 0.4  $\mu$ m<sup>3</sup> on Si (100) substrates in a quartz tube reactor in air atmosphere by the sublimation of molybdenum oxide at T = 660 °C. The phase composition of grown crystals was identified by X-ray single crystal structure analysis.

The layered structure of  $\alpha$ -MoO<sub>3</sub> (orthorhombic phase) consists of double corner-sharing layers of MoO<sub>6</sub> octahedra held together by covalent forces along (100) and (001) directions

<sup>&</sup>lt;sup>a</sup>New Technologies – Research Centre, University of West Bohemia, Univerzitni 8, 306 14 Pilsen, Czech Republic. E-mail: maalidph@yahoo.co.uk; Tel: +420 777729583

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Crystal structure of α-MoO<sub>3</sub> showing the layered structure along the (010) direction. Because of its layered structure and the ease of the Mo(VI)/Mo(V) coupling, α-MoO<sub>3</sub> shows interesting properties for electrochemical devices and displays.





Fig. 1 Fragment of the crystal structure of  $\alpha$ -MoO<sub>3</sub>; (a) crystal structure of  $\alpha$ -MoO<sub>3</sub> showing the layered structure along the (010) direction because of its layered structure and the ease of the Mo(v)/Mo(v) coupling;  $\alpha$ -MoO<sub>3</sub> is of interest in electrochemical devices and displays; (b) elementary unit cell of  $\alpha$ -MoO<sub>3</sub> containing four MoO<sub>3</sub> units; (c) top side view and bottom side view of  $\alpha$ -MoO<sub>3</sub>; (d) front side view and back side view of  $\alpha$ -MoO<sub>3</sub>; (c) left side view and right side view of  $\alpha$ -MoO<sub>3</sub>.

and by van der Waals forces along (010) direction.<sup>19</sup> The octahedra have one short Mo–O bond to non-bridging O.  $\alpha$ -MoO<sub>3</sub> is a yellow or light blue colored crystalline solid that is slightly soluble in acid water.<sup>6</sup>

As mentioned above, it is clear that the previous work were devoted to the synthesis  $\alpha$ -MoO<sub>3</sub> and study of their crystal structure, electronic properties, energy band gap, and chemical bonding; however, there were no reports on the electronic band structure therefore, due to a lack of information regarding the electronic band structure, density of states, electronic charge density distribution and the linear optical properties of  $\alpha$ -MoO<sub>3</sub>,

we addressed ourselves to comprehensive theoretical calculations based on density functional theory (DFT) within an allelectron full potential method. The calculations are performed using four types of exchange correlation potentials within a full potential method to ascertain the effect of exchange correlation on the electronic structure and hence the linear optical properties. In this calculation, we have employed the state-of-the-art all-electron full potential linear augmented plane wave (FPLAPW) method, which has been proven to be one of the most accurate methods for the computation of the electronic structure of solids within DFT.<sup>15-18</sup>

	Lattice constant					
	a (Å) exp.	a (Å) calc.	b (Å) exp.	b (Å) calc.	<i>c</i> (Å) exp.	c (Å) calc.
	13.8674(7)	13.8681 (LDA) 13.9887 (GGA)	3.6976(2)	3.6980 (LDA) 3.8789 (GGA)	3.9644(2)	3.9657 (LDA) 4.0077 (GGA)
	Atomic positions					
	<i>x</i> exp.	x opt. (GGA)	y exp.	y opt. (GGA)	z exp.	z opt. (GGA)
Мо	0.3984(1)	0.3963	1/4	1/4	0.5862(1)	0.5823
01	0.4117(1)	0.4105	1/4	1/4	0.0222(5)	0.0207
O2	0.4357(1)	0.4343	-1/4	-1/4	0.5018(5)	0.5024
O3	0.2782(1)	0.2757	1/4	1/4	0.5346(5)	0.5346



Asymmetric unit of α-MoO<sub>3</sub> with values of interatomic distances (Å) and angles (°).



Fig. 2 (a–b) Asymmetric unit of  $\alpha$ -MoO<sub>3</sub> with values of interatomic distances (Å) and angles (°); (c–d) octahedral MoO<sub>6</sub> building unit with values of interatomic distances (Å) and angles (°). The octahedral MoO<sub>6</sub> contains metal–oxygen bonds whose lengths vary between 1.68 Å and 2.37 Å. The O1 atom is coordinated to one Mo atom with distance of about 1.68 Å, which is in good agreement with the experimental value of 1.67 Å;<sup>28-30</sup> the asymmetric bridging oxygen O2 are situated asymmetrically between two Mo with distances of 1.74 and 2.23 Å, respectively, in good agreement with the experimental values of 1.73 and 2.25 Å.<sup>28-30</sup> The symmetric bridging O3 is located symmetrically between two Mo atoms with a distance of about 2.37 Å, which is in good agreement with the experimental values of 1.94 Å and linked to another Mo atom with a distance of about 2.37 Å, which is in good agreement with the experimental values of 1.94 and 2.33 Å.<sup>28-30</sup>

## 2. Details of calculations

Fig. 1 represents the idealized structure of  $\alpha$ -MoO<sub>3</sub>. The orthorhombic phase of  $\alpha$ -MoO<sub>3</sub> crystallizes in *Pbnm* space group. The geometrical structure of  $\alpha$ -MoO<sub>3</sub> is relaxed by minimizing the forces acting on the atoms (less than 1 mRy/a.u.), using the allelectron full potential linear augmented plane wave (FPLAPW) method as implemented in the WIEN2k code<sup>20</sup> within generalized gradient approximation (PBE-GGA).<sup>21</sup> The experimental lattice constants and the atomic coordinates<sup>14</sup> are listed in Table 1. In comparison with the calculated lattice constants and the atomic coordinates, good agreement was found. The ground state properties of  $\alpha$ -MoO<sub>3</sub> are calculated within four types of exchange correlation potentials. The first three are described by the local density approximation (CA-LDA),<sup>22</sup> PBE-GGA and Engel-Vosko generalized gradient approximation (EVGGA).23 To overcome the underestimation of the band gap of DFT-LDA/ GGA/EVGGA, we also introduced the modified Becke-Johnson potential (mBJ).24 The GGA-mBJ allows the calculation of band gaps with accuracy similar to the very expensive GW calculations.<sup>24</sup> It is a local approximation to an atomic "exactexchange" potential and a screening term. The plane-wave cutoff, defined by the product of the smallest atomic sphere radius and the magnitude of the largest reciprocal-lattice vector ( $R_{\rm MT}$  ×  $K_{MAX}$ ), is considered to be equal to 8. In the muffin-tin (MT) spheres, the potential and charge density are expanded in spherical harmonics with  $l_{\rm max} = 8$  and non-spherical components up to  $l_{\text{max}} = 6$ . In the interstitial region, the potential and the charge density are represented by Fourier series. Selfconsistency is obtained using a  $6 \times 24 \times 22\vec{k}$  points mesh in the irreducible Brillouin zone (IBZ). The self-consistent calculations are converged because the total energy of the system is stable within 0.00001 Ry. The electronic band structure, density of states, electronic charge density distribution, and the linear optical properties are calculated within a 9  $\times$  34  $\times$  31 $\vec{k}$  points mesh in IBZ.

## 3. Results and discussion

## 3.1. Electronic band structure, density of states and the electronic charge density

The dispersion of calculated electronic band structure for α-MoO<sub>3</sub> using mBJ is illustrated in Fig. 3. The calculated band structure within LDA, GGA and EVGGA are reported in the ESI (see Fig. S1<sup>†</sup>). It is clear that the use of different XC pushes the CBM towards higher energies when we move in the order of LDA  $\rightarrow$  GGA  $\rightarrow$  EVGGA  $\rightarrow$  mBJ. Changing exchange correlation (XC) potential has substantial influence on the value of the energy gap. The Fermi level is maintained on zero eV at the top of the valence band maximum (VBM). The conduction band minimum (CBM) is situated at  $\Gamma$  point of BZ, whereas the VBM is located at  $T(-0.5\ 0.5\ 0.5)$  point of BZ, resulting in an indirect band gap of about 2.81 eV, which is in good agreement with the experimental values (3.03 eV, 3.10 eV).6,25 The calculated band gaps within LDA, GGA and EVGGA are presented in the ESI (Table S1<sup>†</sup>). We should emphasize that mBJ succeed by a large amount in bringing the calculated energy gap closer to the experimental one. The value of the energy band gap makes  $\alpha$ -MoO<sub>3</sub> an active visible light catalyst in industrial production.<sup>26</sup>

To comprehensively understand the electronic structures, the total density of states of  $\alpha$ -MoO<sub>3</sub> was determined using LDA, GGA, EVGGA and mBJ, as illustrated in Fig. 4(a), which demonstrates the influences of replacing the exchange correlation potentials on the total density of states. This figure shows that replacing the exchange correlation potentials shifts the structures from CBM and above towards higher energies. This supports our previous finding that mBJ succeeds in bringing the calculated energy gap closer to the experimental one. Therefore, we present the partial density of states of  $\alpha$ -MoO<sub>3</sub> obtained by mBJ in Fig. 4(b-e). The energy region extending between -6.0 eV and Fermi level ( $E_{\rm F}$ ) mainly originates from Mo-d and O1,2,3-p states with small contributions from Mo-s/p and O1,2,3-s states. It is clear that there exists a strong hybridization between Mo-d and O-p states and also between Mo-s/p and O-s states. The energy region from the CBM and above is mainly formed by Mo-d and O1,2,3-p states with small contributions from Mo-s/p and O1,2,3-s states. The CBM is mainly formed by Mo-d state whereas the VBM is a mixture of O1,2,3-p states. The energy region from CBM and above represents a weak hybridization between the states.

The electronic space charge density distribution of  $\alpha$ -MoO<sub>3</sub> is explored to study the origin of chemical bonds between the atoms. The two crystallographic planes, namely (0 0 1) and (1 0 1), are represented in Fig. 5(a) and (b), respectively. It is found that the majority of charges are accumulated on the O site and the distribution of electronic charge is spherical, which



Fig. 3 The calculated electronic band structure of  $\alpha\text{-MoO}_3$  using LDA, GGA, EVGGA and mBJ.



Fig. 4 (a) Calculated total density of states (states per eV per unit cell) using LDA, GGA, EVGGA and mBJ; (b) calculated Mo–s/p partial density of states (states per eV per unit cell) using mBJ; (c) calculated Mo–d partial density of states (states per eV per unit cell) using mBJ; (d) calculated O1,2,3-s partial density of states (states per eV per unit cell) using mBJ; (e) calculated O1,2,3-p partial density of states (states per eV per unit cell) using mBJ; (e) calculated O1,2,3-p partial density of states (states per eV per unit cell) using mBJ; (e) calculated O1,2,3-p partial density of states (states per eV per unit cell) using mBJ; (e) calculated O1,2,3-p partial density of states (states per eV per unit cell) using mBJ.

results in the bonding between Mo–O showing prevailingly ionic and partially covalent features due to the large electronegativity difference between Mo (2.16) and O (3.44). The two crystallographic planes confirm that the valence electrons from the Mo site are transferred to the O site. This can be seen easily by color charge density scale, where blue color (+1.000) corresponds to the maximum charge accumulation site. From the electro-negativity difference one can determine the degree of covalency, which is a very important factor to estimate the hardness of materials.<sup>27</sup>

The interatomic distances (see Fig. 2(a) and c) represent the anisotropic nature of bonds in  $\alpha$ -MoO<sub>3</sub> which is confirmed by



Fig. 5 The calculated electron charge density distribution were calculated in two crystallographic planes; (a) (0 0 1) crystallographic plane of  $\alpha$ -MoO<sub>3</sub>; (b) (1 0 1) crystallographic plane of  $\alpha$ -MoO<sub>3</sub>. Because the crystallographic planes (0 0 1) and (1 0 1) do not show all the details, please refer to Fig. 2 and its caption.

the two crystallographic planes (0 0 1) and (1 0 1). The O1 atom is coordinated to one Mo atom with a distance of about 1.68 Å, which is in good agreement with the experimental value of 1.67 Å;<sup>28-30</sup> the asymmetric bridging oxygens O2 are situated asymmetrically between two Mo with distances of 1.74 and 2.23 Å, respectively, in good agreement with the experimental values of 1.73 and 2.25 Å.<sup>28-30</sup> The symmetric bridging O3 is located symmetrically between two Mo atoms with a distance of about 1.94 Å and linked to another Mo atom with a distance of about 2.37 Å, in good agreement with the experimental values of 1.94 and 2.33 Å.<sup>28-30</sup> The calculated bond distances in comparison with the experimental data<sup>28-30</sup> are listed in Table 2 and illustrated in Fig. 2(a) and (c). In addition, we have calculated the bonds angles as represented in Fig. 2(b) and (d).

#### 3.2. Effective mass

The effective masses and effective mass ratios of  $\alpha$ -MoO<sub>3</sub> compounds can be obtained from the curvature of the valence bands maximum (for the holes) and the conduction band minimum (for the electrons). The effective masses can be obtained through a simple parabolic fitting using the definition of effective mass as a second derivative of energy band with respect to the wave vector, *k*:

 Table 2
 The calculated bond lengths in comparison with the experimental data

	Bond lengths (Å)	
	This work	Other work
Mo-O1	1.68	$1.67^{a,b,c}$
Mo-O2	1.74, 2.23	$1.73^{a,b,c}, 2.25^{a,b,c}$
Мо-О3	1.94, 2.37	$1.94^{a,b,c}, 2.33^{a,b,c}$
<sup><i>a</i></sup> ref. 28. <sup><i>b</i></sup> ref. 29	9. <sup><i>c</i></sup> ref. 30.	

$$\frac{1}{m^*} = \frac{\partial^2 E(k)}{\hbar^2 \partial k^2} \tag{1}$$

The calculated electron effective mass ratio  $(m_e^*/m_e)$ , heavy holes  $(m_{hh}^*/m_e)$  and light holes  $(m_{lh}^*/m_e)$  effective masses ratio of  $\alpha$ -MoO<sub>3</sub> compounds using mBJ are 0.0194, 0.0984 and 0.1034, respectively. It can be assumed that an electron in a solid moves as if it was a free electron but with an effective mass  $m^*$  rather than a free electron mass. The larger the band curvature, the smaller the effective mass. It is quite clear from Fig. 3 that the valence bands are less dispersive in all the high symmetry directions. This would imply larger effective mass for the carriers belonging to these bands and hence low mobility  $\mu_e = e\tau_e/m_e^*$  and  $\mu_h = e\tau_h/m_h^*$ .<sup>31</sup> However, presence of carriers with large mobility is required for obtaining a higher electrical conductivity ( $\sigma = ne(\mu_e + \mu_h)$ ). The electron mobility characterizes how quickly an electron can move through a metal or semiconductor.

#### 3.3. Linear optical response

To obtain the imaginary part of the optical dielectric function's dispersion for the orthorhombic  $\alpha$ -MoO<sub>3</sub>, we need to calculate three tensor components along the polarization directions [1 0 0], [0 1 0] and [0 0 1] with respect to the crystalline axes. These are  $\varepsilon^{xx}(\omega)$ ,  $\varepsilon^{yy}(\omega)$  and  $\varepsilon^{zz}(\omega)$ , which can be evaluated using a formula found in the literature.<sup>32,33</sup> Fig. 6(a) exhibits the imaginary part of the optical dielectric function's dispersion. Broadening is taken to be 0.1 eV, which is typical of the experimental accuracy. The threshold for the optical transitions (optical absorption's edge) between the top of valence band and bottom of conduction band occurs at around 2.81 eV. The  $\varepsilon_2^{xx}(\omega), \ \varepsilon_2^{yy}(\omega)$  and  $\varepsilon_2^{zz}(\omega)$  components display two principle peaks, the highest one is situated around 5.0 eV and the second one is situated around 8.5 eV. The first structure occurs due to the optical transitions between Mo-s/p and O1,2,3-s/p states. The second structure is formed due to the electric-dipole transitions between Mo-s/p and O1,2,3-s/p of the VBs to Mo-p and O1,2,3-p of the CB. It is interesting to highlight that there is a considerable anisotropy between  $\varepsilon_2^{xx}(\omega)$ ,  $\varepsilon_2^{yy}(\omega)$  and  $\varepsilon_2^{zz}(\omega)$ tensor components of the frequency dependent dielectric function. Fig. 6(a) shows that there are two absorption regions, a high absorption region occurs between 2.81 and 6.5 eV and a low absorption region occurs between 8.0 eV and 10.0 eV, where



**Fig. 6** (a) Calculated  $\varepsilon_2^{xx}(\omega)$  (dark solid curve-black color online),  $\varepsilon_2^{yy}(\omega)$  (light dashed curve-red color online) and  $\varepsilon_2^{zz}(\omega)$  (light solid curve-blue color online); (b) calculated  $\varepsilon_1^{xx}(\omega)$  (dark solid curve-black color online);  $\varepsilon_1^{yy}(\omega)$  (light dashed curve-red color online) and  $\varepsilon_1^{zz}(\omega)$  (light solid curve-black color online);  $\varepsilon_1^{GGA}(\omega)$  (light dashed curve-red color online);  $\varepsilon_1^{EVGGA}(\omega)$  (light dotted dashed curve-green color online);  $\varepsilon_1^{mBJ}(\omega)$  (light solid curve-blue color online); (d) calculated  $L^{xx}(\omega)$  (dark solid curve-black color online); (d) calculated  $L^{xx}(\omega)$  (dark solid curve-black color online); (e) calculated  $L^{xx}(\omega)$  (dark solid curve-black color online),  $L^{yy}(\omega)$  (light dashed curve-red color online) and  $L^{zz}(\omega)$  (light solid curve-blue color online); (e) calculated  $R^{xx}(\omega)$  (dark solid curve-black color online),  $R^{yy}(\omega)$  (light dashed curve-red color online) and  $R^{zz}(\omega)$  (light solid curve-blue color online); (f) calculated  $I^{xx}(\omega)$  (dark solid curve-black color online),  $R^{yy}(\omega)$  (light dashed curve-red color online) and  $R^{zz}(\omega)$  (light solid curve-blue color online); (f) calculated  $I^{xx}(\omega)$  (dark solid curve-black color online),  $R^{yy}(\omega)$  (light dashed curve-red color online) and  $R^{zz}(\omega)$  (light solid curve-blue color online); (f) calculated  $I^{xx}(\omega)$  (dark solid curve-black color online),  $R^{yy}(\omega)$  (light dashed curve-red color online) and  $R^{zz}(\omega)$  (light solid curve-blue color online).

the materials exhibit high transparency. The regions confined between 6.5 and 8.0 eV and 10.0 and 13.5 eV are considered as lossless regions.

The real parts  $\varepsilon_1^{xx}(\omega)$ ,  $\varepsilon_1^{yy}(\omega)$  and  $\varepsilon_1^{zz}(\omega)$  of the frequency dependent dielectric function can be obtained with the aid of

Kramers–Kronig relations<sup>33</sup> and the existence information about the imaginary parts  $\varepsilon_2^{xx}(\omega)$ ,  $\varepsilon_2^{yy}(\omega)$  and  $\varepsilon_2^{zz}(\omega)$  of the optical dielectric functions. Fig. 6(b) illustrates the real part that again shows the existence of the anisotropy between the three tensor components.

The calculated values of  $\varepsilon_1^{xx}(0)$ ,  $\varepsilon_1^{yy}(0)$  and  $\varepsilon_1^{zz}(0)$  using mBJ are 4.80, 4.32 and 5.03, respectively. We should emphasize that  $\varepsilon_1(0)$  corresponds to the optical dielectric constant, also known as  $\varepsilon_{\infty}$ . This corresponds only to the electron contribution to the total dielectric constant. The uniaxial anisotropy  $\delta \varepsilon = [(\varepsilon_0^{\rm II} - \varepsilon_0^{\perp})/\varepsilon_0^{\rm tot}] =$ 0.154, indicating the existence of considerable anisotropy between the parallel  $(\varepsilon_2^{II}(0) = \varepsilon_1^{zz}(0))$  and the perpendicular  $\left(\varepsilon_2^{\perp}(0) = rac{\varepsilon_1^{xx}(0) + \varepsilon_1^{yy}(0)}{2}
ight)$  polarization directions. The calculated values of  $\varepsilon_1^{xx}(0)$ ,  $\varepsilon_1^{yy}(0)$ ,  $\varepsilon_1^{zz}(0)$  and  $\varepsilon_1^{av}(0)$  within LDA, GGA and EVGGA are presented in the ESI.<sup>†</sup> We would like to demonstrate the influence of the exchange correlation potential on the value of the energy gap and hence on the optical properties. Therefore, we plot the average of the real parts  $\varepsilon_1^{av}(\omega)$  obtained from LDA, GGA, EVGGA and mBJ in Fig. 6(c), which shows that mBJ gives the lowest values. We note that a smaller energy gap yields a larger  $\varepsilon_1(0)$  value. This could be explained on the basis of the Penn's model.<sup>34</sup> Penn proposed a relation between  $\varepsilon(0)$  and  $E_g$ ,  $\varepsilon(0) \approx 1 + (\hbar \omega_{\rm P}/E_{\rm g})^2$ .  $E_{\rm g}$  is some kind of averaged energy gap that could be related to the real energy gap. It is clear that  $\varepsilon(0)$  is inversely proportional to  $E_{g}$ . Therefore, a larger  $E_{g}$  yields a smaller  $\varepsilon(0)$ .<sup>35,36</sup> This finding support our previous observation from the calculated electronic band structure and the density of states, which shows that LDA, GGA and EVGGA underestimate the energy band gap, while mBJ succeeded in bringing the calculated energy band gap closer to the experimental one.

The other optical properties, such as reflectivity spectra  $R(\omega)$ , absorption coefficient  $I(\omega)$  and the electron loss function  $L(\omega)$ , can be evaluated with the aid of the existing information on the calculated imaginary and real parts of the frequency dependent dielectric function. Fig. 6(d) illustrates the loss function  $L(\omega)$ , which confirms the existence of the lossless regions 6.5–8.0 eV and 10.0–13.5 eV, which is in agreement with our observation in Fig. 6(a). The peaks of loss function represent the plasma frequencies ( $\omega_P$ ). We should emphasize that above  $\omega_P$ , the material behaves as dielectric, where  $\varepsilon_1(\omega)$  is positive, while below  $\omega_P$ , where  $\varepsilon_1(\omega)$  is negative, the material exhibits a metallic nature.

Fig. 6(e) illustrates the optical reflectivity  $R(\omega)$  as a function of photon energy. It is clear that at low energies  $\alpha$ -MoO<sub>3</sub> compound exhibits a low reflectivity of about 17.0%, which then gradually increases to reach 50%, forming the first reflectivity maximum at about 5.0 eV. The first reflectivity minima occurs between 6.5 and 8.0 eV confirming the occurrence of a collective plasmon resonance. The depth of the plasmon minimum is determined by the imaginary part of the frequency dependent optical dielectric function at the plasma resonance and is representative of the degree of overlap between the inter-band absorption regions. Fig. 6(f) represents the absorption coefficient  $I(\omega)$  of  $\alpha$ -MoO<sub>3</sub>; it shows that there are two absorption bands, the first one extends between 2.81 and 6.5 eV and the second one between 8.0 eV and 13.5 eV in which the crystal exhibits high transparency.

## 4. Conclusions

The electronic band structure, density of states, electronic charge density distribution, chemical bonding and the linear

optical properties of the orthorhombic molybdenum trioxide  $\alpha$ -MoO<sub>3</sub> were calculated. We employed density functional theory based on an all-electron full potential linear augmented plane wave (FPLAPW) method as implemented in the WIEN2k code within four types of exchange correlation potentials. Calculation demonstrated that  $\alpha$ -MoO<sub>3</sub> is an indirect band gap insulator. The CBM is situated at  $\Gamma$  point of BZ, whereas the VBM is located at T point of BZ. The calculated electronic band structure and the total density of states confirmed that mBJ brings the calculated energy band gap (2.81 eV) closer to the experimental one (3.03 eV and 3.1 eV). The electronic space charge density distribution of α-MoO<sub>3</sub> was explored in two crystallographic planes  $(0 \ 0 \ 1)$  and  $(1 \ 0 \ 1)$  to study the origin of the chemical bonds. It is found that the majority of the charges are accumulated on the O site and the distribution of electronic charge is spherical. The two crystallographic planes confirm that valence electrons from the Mo site are transferred to O site.

The interatomic distances represent the anisotropic nature of the bonds in  $\alpha$ -MoO<sub>3</sub>, which is confirmed by the two crystallographic planes (0 0 1) and (1 0 1). The calculated bond distance is in very good agreements with the experimental data. The optical properties are calculated for three tensor components along the polarization directions [1 0 0], [0 1 0] and [0 0 1] with respect to the crystalline axes. It is found that the regions confined between 6.5 and 8.0 eV and 10.0 and 13.5 eV are considered as lossless regions. The calculated optical properties support our previous observation from the calculated electronic band structure and the density of states, which showed that LDA, GGA and EVGGA underestimate the energy band gap, while mBJ succeeded in bringing the calculated energy band gap closer to the experimental one.

### Associated content

Full information about the calculated electronic band structures of  $\alpha$ -MoO<sub>3</sub> using; (a) LDA; (b) GGA; (c) EVGGA; (d) mBJ. The calculated energy band gaps in comparison with the experimental value. The calculated  $\varepsilon_1^{xx}(0)$ ,  $\varepsilon_1^{yy}(0)$ ,  $\varepsilon_1^{zz}(0)$  and  $\varepsilon_1^{av}(0)$  of  $\alpha$ -MoO<sub>3</sub> using; (a) LDA; (b) GGA; (c) EVGGA; (d) mBJ.

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